Monthly Notices of the ROYAL ASTRONOMICAL SOCIETY

MNRAS **505**, 3452–3469 (2021) Advance Access publication 2021 May 27

https://doi.org/10.1093/mnras/stab1531

This article has been accepted for publication in Monthly Notices of the Royal Astronomical Society at https://doi.org/10.1093/mnras/stab1531. © 2021 The Authors. Published by Oxford University Press on behalf of the Royal Astronomical Society. All rights reserved.

The evolution of rapid optical/X-ray timing correlations in the initial hard state of MAXI J1820+070

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Accepted 2021 May 17. Received 2021 April 26; in original form 2021 March 2

ABSTRACT

We report on a multiepoch campaign of rapid optical/X-ray timing observations of the superbright 2018 outburst of MAXIJ1820+070, a black hole low-mass X-ray binary system. The observations spanned 80 d in the initial hard state and were taken with NTT/ULTRACAM and GTC/HiPERCAM in the optical ($u_sg_sr_si_sz_s$ filters at time resolutions of 8–300 Hz) and with ISS/NICER in X-rays. We find (i) a growing anticorrelation between the optical and X-ray light curves, (ii) a steady, positive correlation at an optical lag of ~0.2 s (with a longer lag at longer wavelengths) present in all epochs, and (iii) a curious positive correlation at *negative* optical lags in the last, X-ray softest epoch, with longer wavelengths showing a greater correlation and a more negative lag. To explain these, we postulate the possible existence of two synchrotron-emitting components – a compact jet and a hot flow. In our model, the significance of the jet decreases over the outburst, while the hot flow remains static (thus, relatively, increasing in significance). We also discuss a previously discovered quasi-periodic oscillation and note how it creates coherent optical time lags, stronger at longer wavelengths, during at least two epochs.

Key words: accretion, accretion discs – X-rays: binaries – X-rays: individual: MAXI J1820+070 – black holes.

1 INTRODUCTION

Low-mass X-ray binaries (LMXBs) are highly variable systems involving accretion on to either a neutron star or a black hole. Over the past few decades, there have been many efforts to study this variability and detail its behaviour, and there is an expanding body of literature detailing this (see Belloni & Hasinger 1990a; Mushotzky et al. 1993; van der Klis 2000, and many others). But why is the study of this variability important?

In short, because these systems are complex and unresolvable with current telescopes. LMXBs host a compact object accreting via a disc of material transferred from a Roche lobe-filling companion star. The environment is complex, with an outer disc, hot inner flow/corona, and compact, relativistic jets (to name just a few), which all emit across the electromagnetic spectrum. And, during transient, violent outbursts that occur every few years or decades and can last for weeks to months, the scale, presence, and behaviour of these regions can change significantly. Their compact nature means that physically important time-scales can span approximately microseconds in the inner zones to decades at the other extreme. The goal of multiwavelength timing studies of these sources is to understand the physical processes in these components and thus the system as a whole.

Over the relatively short history of multiwavelength astronomy, better technology and new telescopes have improved the temporal resolution of such studies, and with it, our understanding has advanced; Motch, Ilovaisky & Chevalier (1982), Motch et al. (1983), and Imamura, Steiman-Cameron & Middleditch (1987) were some of the earliest reports on rapid stochastic multiwavelength variability down to millisecond scales, while Kanbach et al. (2001) was one of the works that showed intriguing relations between the rapid optical and X-ray variability for the first time. This inter-band relationship was then found to vary between systems, each time showing complex

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behaviour, interpreted as a varying dominance of the inflowing or outflowing plasma through the disc, the inner flow, and the jet (e.g. Durant et al. 2008; Gandhi et al. 2008; Casella et al. 2010; Gandhi et al. 2010; Durant et al. 2011; Gandhi et al. 2017; Pahari et al. 2017). The true importance of these studies is in providing novel quantitative constraints of the physical scales and interactions between the accreting plasma components. For instance, a rapid optical/infrared lag of ~ 100 ms relative to X-rays has now been observed in several systems and appears to be an important constraint for models of jet launching and acceleration (Gandhi et al. 2017).

Yet, these studies rely on the source being both sufficiently bright and well observed at multiple wavelengths simultaneously, the former being rare and the latter being marred by the inherent unpredictability of these outbursts. As such, these studies have so far been few and far between and rarely carried out multiple times over the same outburst – though there are hints at an evolution of processes at different stages of the outburst (see e.g. Veledina et al. 2017; Vincentelli & Casella 2019, though note that the latter compares two different outbursts). Solutions are not yet unique, with processes such as a jet and a hot flow invoked to explain certain signatures on intermediate time-scales (e.g. Veledina, Poutanen & Vurm 2013a; Malzac et al. 2018). We still remain severely data-limited in terms of high-quality strictly simultaneous multiwavelength time series in order to make progress.

In 2018, one particular X-ray binary was discovered. It became bright enough and observed well enough that a good picture of its initial, several-week-long hard state – including evolving inter-band correlations and Fourier components, observed at over 100 Hz – has been made possible.

Discovered first as optical transient ASASSN-18ev on 2018 March 6 (Denisenko 2018; Tucker et al. 2018) and then as an X-ray source on March 11 (Kawamuro et al. 2018), MAXI J1820+070 (hereafter J1820) was detected during the rapid outburst rise. It quickly rose to a brightness of \sim 4 Crab (Shidatsu et al. 2019), becoming the brightest extra-solar object in the X-ray sky by the time it peaked on March 23 (Corral-Santana et al. 2016). By this point, its brightness had led to observations at many sites (e.g. Baglio, Russell & Lewis 2018; Bahramian, Strader & Dage 2018; Bright, Fender & Motta 2018; Del Santo & Segreto 2018); not only did these observations quickly identify it as a likely black hole low-mass X-ray binary (LMXB) (Baglio et al. 2018; Bright et al. 2018; Uttley et al. 2018) but they also revealed rapid optical flaring (Littlefield 2018; Sako et al. 2018) and even a significant optical/X-ray correlation (Paice et al. 2018). Later, a quasi-periodic oscillation (QPO) would be first identified in this source at around this peak (Mereminskiy et al. 2018; Yu et al. 2018) and would be seen to evolve over the next few months (Stiele & Kong 2020). This stage of the outburst was the 'hard state', where it is believed that the inner edge of the accretion disc is recessed and a relativistic jet is present (Done, Gierliński & Kubota 2007).

After the peak, J1820 entered a gradual decline in X-ray flux. In early 2018 July, it transitioned rapidly to the soft state (Homan et al. 2018), where the accretion disc extends to the innermost stable circular orbit (ISCO) and the jet is quenched. During this time, a unique blackbody X-ray emission signature was detected, which has been suggested as originating from within the ISCO, the so-called 'plunge region' (Fabian et al. 2020). J1820 remained in this state until late 2018 September, when it transitioned back to the hard state (Negoro et al. 2018). It has since undergone a series of small 'rebrightenings' (Hambsch et al. 2019; Tomsick & Homan 2019; Ulowetz, Myers & Patterson 2019; Xu, Harrison & Tomsick 2019; Zampieri et al. 2019; Adachi et al. 2020), but as of yet, it has not undergone a second outburst. Fig. 1 shows a timeline of the hard



Figure 1. Timeline of MAXI J1820+070's 2018 outburst. Vertical black dashed lines denote dates of observations (see Table 1). The source transitions to the soft state just after MJD 58300. *Swift*/XRT fluxes and photon indices were obtained from spectra produced by *Swift*'s 'Build XRT Products' tool (Evans et al. 2009), using only data that correspond to our epochs; errors are smaller than the marker size for both data sets. *Top*: Continuous monitoring done by *Swift*/BAT (filled blue circles) and ISS/MAXI (open red circles). *Middle*: X-ray fluxes from *Swift*/XRT (purple triangles). Also plotted are radio luminosities from AMI-LA (orange diamonds), presented in Bright et al. (2020). *Bottom*: Photon indexes (black squares).

state outburst at X-ray and radio wavelengths, using data from the Neil Gehrels *Swift* Observatory, MAXI, and AMI-LA.

Radio parallax measurements have since constrained J1820 to a distance of 2.96 ± 0.33 kpc (Atri et al. 2020), and the optical parallax found using *Gaia* EDR3 (Gaia Collaboration et al. 2020) gives a distance of $2.94^{+0.87}_{-0.55}$ kpc (calculated using the recommended zeropoint correction – Lindegren 2020), which improves on the previous estimate reported in *Gaia* DR2 (Gandhi et al. 2019).

J1820's brightness led to several multiwavelength campaigns using high-time-resolution instrumentation over the course of its outburst. In Paice et al. (2019), we discussed the optical/X-ray correlations taken from a single night, using HiPERCAM and NICER during the rising hard accretion state. Therein, we noted the presence of a sub-second optical lag of order $\sim 100 \text{ ms}$ between the bands dependent upon wavelength, which we attributed to structure within the compact jet, and presence of an anticorrelation, which we put in the context of the hot accretion flow. Together with GX 339–4 and V404 Cyg (Gandhi et al. 2017), these results make J1820 the third well-studied black hole XRB to show the aforementioned sub-second lag.

The above results all highlight the importance of J1820 as a benchmark for understanding accretion. Here, we expand on these results to trace the timing properties through the primary hard state, including four new observations between NICER and another optical instrument, ULTRACAM, as well as a second correlated HiPER-

Epoch	UT date	Day Num. ^a	Time start (MJD-58000) ^b	Time End (MJD-58000) ^b	Optical instrument	X-ray instrument	Optical filters	Correlated time (s)	Cadence (ms) ^c
1	2018-03-16	5	193.38035	193.38518	ULTRACAM	NICER	$u_{\rm s}g_{\rm s}r_{\rm s}$	417	13.8 (138)
2	2018-03-22	11	199.34590	199.41903	ULTRACAM	NICER	$u_{\rm s}g_{\rm s}i_{\rm s}$	1279	9.06 (27.2)
3	2018-04-12	32	220.40479	220.40736	ULTRACAM	NICER	$u_{\rm s}g_{\rm s}i_{\rm s}$	222	10.4 (31.1)
4	2018-04-17	37	225.17310	225.25110	HiPERCAM	NICER	$u_{\rm s}g_{\rm s}r_{\rm s}i_{\rm s}z_{\rm s}$	1648	2.93
5	2018-04-17	37	225.30454	225.31547	ULTRACAM	NICER	$u_{\rm s}g_{\rm s}i_{\rm s}$	780	23.0 (69.0)
6	2018-06-07	88	276.19520	276.22171	HiPERCAM	NICER	$u_{\rm s}g_{\rm s}r_{\rm s}i_{\rm s}z_{\rm s}$	1196	2.93

Table 1. Log of simultaneous ULTRACAM/HiPERCAM & NICER observations for MAXI J1820+070 2018 hard state outburst.

^aNumber of days since 2018 March 11 (MJD 58188), as used by Stiele & Kong (2020).

^bStart and end of simultaneous times only – observations may contain gaps.

^cLimiting cadences in optical. Numbers in brackets are u_s -band cadences, if different from the other bands.

CAM/NICER observation later in the outburst. All observations were taken during the initial hard state cover time resolutions from 8 Hz to 300 Hz and cover a span of roughly 80 d in total. We construct a picture of the evolving optical/X-ray correlations over this period and discuss to what processes they may relate.

2 OBSERVATIONS

2.1 NTT/ULTRACAM - optical

ULTRACAM is a fast-timing optical camera on the 3.58-m New Technology Telescope (NTT) in La Silla, Chile. It was built for the purpose of fast optical timing in multiple wavebands. To this end, it includes three channels for simultaneous multiwavelength monitoring (with replaceable filters). It can also observe at frame rates well above 100 Hz; this is achieved by the lack of a physical shutter and frame transfer CCDs that can rapidly shift charge into a storage area for reading out, freeing up the original pixels for observation, and thereby achieving low dead times (Dhillon et al. 2007).

We used ULTRACAM to observe J1820's initial outburst peak in the early mornings of 2018 March 16, March 22, April 12, and April 17. All observations were carried out with the u_s , g_s , and i_s SDSS filters, except for the first, which used the r_s filter instead of i_s . Unlike most observations of this type, the times were not explicitly chosen to coincide with X-ray observations – instead, the overlaps were purely coincidental and the serendipitous result of near-constant monitoring of J1820 by multiple telescopes. ULTRACAM was used in two-window mode (one each for the target and comparison star), with both window sizes of 50 × 50 pixels with a 2 × 2 binning for sensitivity and speed. See Table 1 for observational details. J1820 was very faint in u_s , and so ULTRACAM's on-chip co-adding feature was used; this provides a longer exposure time in u_s so as to increase signal-to-noise ratio.

The data were reduced using the ULTRACAM pipeline v9.14 (Dhillon et al. 2007). The bias was subtracted from each frame, and flat-field corrections were also applied. Aperture sizes scaled to the instantaneous seeing were used, with radii between 0".7 and 3".5, with an annulus between 12" and 6".3 to calculate the background. These apertures had variable centre positions that tracked the centroids of the sources on each frame, with a two-pass iteration (where an initial pass is made to track the sources on the CCD before a second photometry pass) used for accuracy. Our times were then adjusted to barycentric dynamical time (BJD_TDB) using methods given in Eastman, Siverd & Gaudi (2010).

Our comparison star is located at RA = 18 20 26.43, Dec = 07 10 11.7 (J2000), and is listed in the PANSTARRS survey catalogue (Magnier et al. 2020) with $g_s li_s$ magnitudes of 13.3083/12.233,

respectively. The star was taken to be constant and was used for photometric calibration. For the u_s observations, the comparison star was too faint to perform photometry within a single frame. Hence, we used the measured zero-point magnitude for the u_s band in photometric conditions for ULTRACAM (Vik Dhillon, priv. communication) in order to calibrate our observations. We extracted the J1820 and comparison star magnitudes using aperture photometry with a variable aperture size that was dictated by the seeing conditions. The aperture also tracked the centroid of the source of interest by using a bright star in the field as a reference. For the u_s observations, we used J1820 as the reference object itself so as to not lose tracking within the field.

2.2 GTC/HiPERCAM - optical

High-speed multicolour photometry of J1820 was carried out using HiPERCAM (Dhillon et al. 2018) on the 10.4-m Gran Telescopio Canarias on La Palma. HiPERCAM uses four dichroic beamsplitters to image simultaneously five optical channels covering the $u_sg_sr_si_sz_s$ bands (central wavelengths 3526, 4732, 6199, 7711, and 9156 Å, respectively). The CCDs were binned by a factor of 8 and used in the highest speed drift mode. We orientated the instrument (PA = 58°) and used two windows (96 × 72 pixels each), one centred on J1820, and another on a comparison star, APASS–34569459 (Henden et al. 2015). The observations discussed here were taken on 2018 April 17 from 03:26 to 06:11 UT, and on 2018 June 7 from 04:41 to 05:39, coordinated with NICER. The exposure time was 2 ms, the cadence 2.9 ms, and the median seeing 2.2″. The sky was affected by mild cirrus on both dates.

We used the HiPERCAM pipeline software¹ to de-bias, flat-field, and extract the target count rates using aperture photometry with a seeing-dependent circular aperture tracking the centroid of the source. Sky background was removed using the clipped mean of an annular region around the target. The target was brighter than all stars in the field. We thus used the raw target counts for the analyses presented herein; note that our primary results are not affected when using photometry relative to the comparison star.

2.3 ISS/NICER - X-ray

NICER (Neutron star Interior Composition ExploreR) is an X-ray instrument aboard the International Space Station (ISS). It comprises 52 functioning X-ray concentrator optics and silicon drift detector pairs, arranged in seven groups of eight. Individual photons between

¹https://github.com/HiPERCAM/hipercam

0.2 and 12 keV, and their energies, can be detected to a time resolution of 40 ns (Gendreau et al. 2016).

J1820 was observed with an intensive monitoring program during the initial hard state of its outburst. Data reduction of ObsIDs 1200120105, 1200120107, 1200120127, 1200120131, and 1200120172 was completed using NICERDAS, a collection of NICER-specific tools, and part of HEASARC.² Full level 2 calibration and screening was conducted with *nicerl2*, which calibrated, checked the time intervals, merged, and cleaned the data. Barycentric correction was carried out using BARYCORR, and then the photon events (all between 0.2 and 12 keV) were binned to the times of the optical light curve.

3 METHOD

Our analysis of the optical and X-ray data involves creating simultaneous light curves, cross-correlation functions (CCFs), and Fourier analysis. In the following, we detail the methodology used.

3.1 Simultaneous light curves

Simultaneous light curves are plotted in Fig. 2. The optical and X-ray data are not, by default, binned simultaneously. However, while the optical data were taken in discrete time bins by both instruments, NICER is a photon-counting instrument and thus records the arrival time of each photon. Therefore, we create simultaneous light curves by binning the photons directly to the optical time bins, after barycentring both data sets. Since the optical light curves have a constant dead time (time between the bins in which no data were recorded), the X-ray photons observed during this time are disregarded. For X-rays, the square root of the counts per bin was used to determine the error for each bin. Since the u_s band data were sampled at a different rate to the other optical bands, a separate X-ray light curve was created. This light curve is not plotted in Fig. 2 but was used in creating the CCFs and in the Fourier analysis for the u_s -band data in epochs 1–3 and 5.

3.2 Cross-correlation functions

Cross-correlations are plotted in Figs 3 and 4. Cross-correlations are measurements of how much one light curve (or any time series) varies dependent on another as a function of lag. In these cases, we create optical versus X-ray cross-correlations; the figures therefore show the response of the optical light curves to variations in the X-ray light curve, as a function of time lag. Positive values indicate a net correlation at that lag, and negative values a net anticorrelation, each normalized so that 1 and -1 indicate perfect correlations and anticorrelations.

The cross-correlations were produced by splitting the simultaneous light curves into segments of equal length. Each segment was then 'pre-whitened' by removing a linear trend. A CCF was then run on each segment, using the methodology of Venables & Ripley (2002, p. 390). The mean CCF was then determined and the standard error on each bin was calculated. To probe variations on different time-scales, we compute CCFs using segment sizes of 10 s (Fig. 3) and 2 s (Fig 4).

3.3 Fourier analysis

Fourier analysis is presented in Figs 5–8. These involved computing the Fourier transform of the light curves and then analysing them at each frequency.

The power spectra represent the amplitude of the variability at each Fourier frequency. The coherence represents the relative magnitude of the complex-valued cross-spectrum, i.e. a measure of how the bands are correlated at that frequency. The phase lags represent the relative phase angle of the complex-valued cross-spectrum, i.e. a measure of the lag between the bands at each frequency as a function of phase (measured in radians). The time lags show the same data as the phase lags but converted into the time domain.

This analysis made use of the Stingray³ PYTHON package (Huppenkothen et al. 2019). Values for the intrinsic coherence, and errors on those values, were determined using methods described in equation (8) of Vaughan & Nowak (1997), where our data fit into the category of 'High powers, high measured coherence'.

Good time intervals were used based on the individual epochs of X-ray observation, and then cross-spectra were computed over independent light curve segments and averaged. The segment lengths were 2^{12} bins for epochs 1–3 and 5, and 2^{14} bins for epochs 4 and 6. For observations with co-adding in u_s , the nearest multiple of 2 was used as the bin length, so that the light-curve segments were of similar size compared to the other filters of the same observation. These segment sizes were selected to balance frequency range against statistics, making sure that all bands were averaged over at least five segments (aside from the u_s bands in epoch 3 and 5, which had only three and four segments, respectively).

Root-mean-squared (rms²) normalization was applied to the power spectra (Belloni & Hasinger 1990b). The white noise was fitted and removed from the power spectra before calculating the coherence (see Section 4.3.1 for details). In Figs 5–8, the frequency-dependent products were binned logarithmically in frequency; for the power spectra, the factor was 1.1, while for the coherence, time lags, and phase lags, the factor was 1.3 (these were chosen to balance the clarity of features with the size of the uncertainties).

Time lags were calculated by dividing the phase lags by $2\pi f$, where f is the frequency of the bin. Since the conversion is ambiguous and could be $\pm 2\pi$, we assumed that the phase lags of the frequency bins around 1 Hz were correct, based on their relationship to the subsecond time lag seen in Fig. 4. Each time lag was then arbitrarily shifted based on what would cause the fewest discontinuities.

4 RESULTS

In Figs 2–8, the violet plot on the left shows the timeline of the outburst in MJD, seen by *Swift*/BAT (see Fig. 1) – the stronger the colour, the brighter J1820 was in hard X-rays. The epochs are marked. Each plot shows the variation in all bands. The colour key is as follows: u_s (blue), g_s (green/teal), r_s (red), i_s (dark red/brown), z_s (black), and X-rays (violet).

4.1 Light curves

Fig. 2 shows portions of the light curves from each of the epochs in all optical bands as well as in X-rays. The light curves show a lot of similarities – in the optical, there are numerous sub-second flares with an increase of a factor of $\sim 1.5-2$ in flux. A common property of

³https://github.com/StingraySoftware/stingray



Figure 2. Portions of optical and X-ray light curves from each epoch, normalized to each band's mean. *Far Left*: Timeline of the outburst in MJD, seen by *Swift*/BAT (stronger colour = brighter in hard X-rays). *Left*: 60-s overview, binned to show overall variations. *Right*: 4-s insets, marked by dotted lines in the left. Arbitrary offsets have been applied to the time axis. The u_s band for Epoch 6 suffered from poor statistics and was thus not plotted.



0.1 58200 - 2 0 -0.1 0.2 58210 0.1 0 58220 -0.1 2 • 3 0.2 ₹₹₹ •4/5 0.1 58230 0 -0.1 0.2 58240 0.1 0 58250 -0.1 0.2 Ŧ Ŧ 0.1 58260 0 -0.1 0.2 58270 0.1 ÿ • 6 0 58280 -0.1 -1 -0.5 0.5 0 1 Lag (s)

Figure 3. Optical/X-ray cross-correlation functions (i.e. a peak/trough at positive lags means that the optical flux lags the X-ray flux). The CCFs shown are the average CCF computed from multiple 10-s segments. The light curves were binned to roughly match the lowest time resolution (epoch 5, 43 Hz) in order to better compare CCF coefficient values (except for u_s in epochs 1–3 and 5, due to their significantly lower time resolution). Standard errors, averaged over the plotted range, are shown. *Far left*: Timeline of the outburst – see Fig. 2 caption.

Figure 4. Same as in Fig. 3, but the CCFs are created from 2-s segments instead. This allows us to better compare the rapid variability and shows that the sub-second peak at positive lags is present in a similar place in every single band and epoch.



Figure 5. Power spectra of J1820. White noise has been fitted and removed from each. *Far left*: Timeline of the outburst – see Fig. 2 caption.



Figure 6. Coherence of J1820 over frequency, with the same rebinning as in Figs 5 and 8.





Figure 7. Phase lags of J1820 over frequency, with the same rebinning as in Figs 5 and 8.

Figure 8. Time lags of J1820 over frequency. Inset for each plot shows a linear version of the region around the 0.2-s lag seen in the CCFs. Open circles denote negative optical time lags.

Epoch	X-rays	us	gs	rs	is	Zs
1	2; 36.6 (1.47)	2; 59.4 (0.561)	2; 6.19 (0.847)	2; 4.02 (1.43)		
2	2; 36.9 (1.4)	4; 84.2 (1.13)	4; 6.95 (2.84)		4; 3.52 (1.69)	
3	2; 11.7 (0.992)	2; 26.0 (0.495)	4; 5.79 (1.08)		4; 3.92 (0.894)	
4	5; 15.4 (0.86)	3; 0.77 (2.07)	6; 0.09 (3.98)	6; 0.11 (4.98)	7; 0.14 (7.77)	8; 0.23 (8.93)
5	2; 11.5 (1.16)	2; 32.8 (0.484)	4; 5.8 (0.762)		4; 3.25 (1.34)	
6	5; 29.6 (1.66)	2; 324 (0.65)	4; 0.38 (2.56)	4; 0.57 (2.76)	4; 0.66 (2.71)	4; 10.1 (4.28)

Table 2. Fitting parameters for the power spectra. Each cell contains the following: number of Lorentzians fitted; white noise level in fractional rms² units $\times 10^{-5}$ (reduced $\chi^2 \chi^2_{\nu}$).

all light curves is that the variations tend to be far stronger in the red than in the blue and is particularly true of the sub-second flares – this is also seen in other hard-state LMXBs (Gandhi et al. 2010, 2016). These flares become less frequent as the epochs continue but are still present in epoch 6. Interestingly, the light curves are sometimes anticorrelated during these flares, with optical activity rising while X-ray activity decreases – see, for example, the inset to epoch 4.

4.2 Cross-correlation functions

CCFs from 10-s segments can be seen in Fig. 3. Each epoch shows a sub-second correlation peak. Epochs 1–5 also show some form of a 'precognition dip'; i.e. an anticorrelation at negative lags, which means that either the optical light curve dips a few seconds before an X-ray flare or that optical flares occur before an X-ray dip.

We can also see how the CCFs evolve over time. Between epochs 1–5, the correlation steadily decreases at positive lags, perhaps caused by an anticorrelation component becoming more significant in the data. Additionally, from epoch 3 onwards, a new positively correlated component appears, peaking at negative lags, which is stronger at longer wavelengths. This feature evolves from \sim -3 s in epoch 3 to -1 s in epoch 6.

To probe the more rapid variations, we also created CCFs from 2-s segments, which can be seen in Fig. 4. These reveal several details. First, the sub-second correlation is strongest just before the peak of the outburst. Secondly, the lag of the CCF peak is fairly constant from epoch 2 onwards, even into epoch 6. Finally, the CCF peak has a 'tail' extending from the initial peak out to 0.5–0.75 s and appears to shrink over time, or at least become less significant compared to some anticorrelated component; see, in particular, the difference between epochs 4 and 6.

The sub-second correlation was previously reported in Paice et al. (2019). In that work, we found that the lag was greater at longer wavelengths – this can be seen in several of these epochs, and will be shown more explicitly in Section 4.3.4, and finally discussed in Section 5.1. Our highest resolution epochs, 4 and 6, also show a small spike in the CCF at 0-s lag. This is confirmed by CCFs created from 1-s light-curve segments and below. However, our data do not have sufficient time resolution to study these particular features.

A closer inspection shows that the correlated negative-lag component is present in epoch 6 but with curious results. First, the peak is now at 0 s, not -1 s. Secondly, at negative lags, the longer wavelengths have a stronger correlation, while the shortest wavelength (u_s) shows a trend towards anticorrelation. At positive lags, the reverse is true; it is the longer wavelengths that now show a trend towards anticorrelation. This shows that either this negative component affects the signals down to these rapid time-scales or there are two components that affect these lags – this correlated negative component and a new component that has appeared between epochs 5 and 6. These possibilities will be discussed in Sections 4.4 and 4.5.

4.3 Fourier analysis

To better understand the nature of different components contributing to the CCF, we perform the decomposition of the observed variability into different time-scales using Fourier technique. Figs 5–8 show various Fourier components in each optical band plotted against X-rays.

4.3.1 Power spectra

The power spectra can be seen in Fig. 5. In addition to the five optical bands (detailed at the beginning of Section 4), the X-ray power spectra are also shown⁴ and not the full spectra from the NICER observations. Thus, these are not directly comparable to the power spectra in Stiele & Kong (2020). The power is in fractional rms² units and is multiplied by the frequency.

As noted in Section 3.1, the separate X-ray light curves for the co-added u_s bands in epochs 1–3 and 5 are not shown. Additionally, the u_s power spectrum in epoch 6 is not shown due to the poorer data quality.

A mix of zero-centred and non-zero-centred Lorentzians along with a constant white noise component was fitted to each band. For these plots, that white noise component was removed and the fitted parameters can be seen in Table 2. The increased numbers of Lorentzians (and increased χ^2_{ν} values) for epochs 4 and 6 are due to the higher cadences, larger segment sizes, and lower noise levels in the HiPERCAM data; these lead to far lower uncertainties and thus require more Lorentzians to fit numerous features in these bands.

Regarding the evolution of the power: In all epochs, the power in the optical bands is consistently higher at longer wavelengths, although highest overall in X-rays. The manifestation of this can be seen in Fig. 2, where one can see activity at longer wavelengths being much stronger than that at shorter ones.

The power in each band evolves over the course of the outburst. At optical wavelengths, the power above $\sim 3 \text{ Hz}$ drops between epochs 1 and 6 by almost an order of magnitude. This is most evident when looking at 10 Hz in the *i*s-band power spectrum. However, at the lowest frequencies, it appears more stable. This could be interpreted as a Lorentzian component peaking at $\sim 1-2$ Hz and becoming less significant as the outburst continues. However, this does not mean that the component disappears. Furthermore, a small feature is seen to peak at $\sim 30-40$ Hz in all optical bands in epochs 4 and 6 (the only bands that extend to this frequency with good statistics. Epochs 2 and 3 may show this too, but the uncertainties are too large to confirm this).

Meanwhile, the X-ray power spectrum behaves in the opposite manner. It remains roughly constant between epochs at all frequen-

⁴Note that these are only for the X-ray data that are strictly simultaneous with our fast optical photometry (aside from the u_s band in cases of co-adding, i.e. epochs 1–3 and 5).

cies except the lowest, where it drops by an order of magnitude between the earliest and latest epochs.

All the power spectra show a break at around 1 Hz, and epochs 4 and 6 possibly show higher frequency breaks at around 40 Hz. However, Lorentzian fitting could not sufficiently quantify these breaks, and therefore their validity and cause will instead be left as a topic for future work.

Regarding the existence of a quasi-periodic oscillation: In epochs 4 and 5, a QPO-like feature can be seen at ~ 0.1 Hz. While Lorentzian fitting did not significantly improve with an additional component at these frequencies for all bands, an X-ray QPO at these frequencies has been previously detected; the existence and effects of such a feature are discussed in Section 4.4.

4.3.2 Coherence

Fig. 6 shows the coherence. Overall, this is generally low (<0.1) at all frequencies, which is typical for these sources (see e.g. Malzac et al. 2018). During all epochs and bands, the optical is more coherent with the X-rays at lower frequencies and decreases with increasing frequency in every epoch. However, the coherence at lower frequencies decreases as the outburst continues, eventually dropping by over an order of magnitude by epoch 6.

There are numerous smaller features here, but for this work, we will just note the peaks that occur in the later epochs - at 0.1 Hz in epochs 4 and 5, and at 0.3 Hz in epoch 6. These will be referred to later in Section 4.4 in the context of a QPO.

While there is no one relation for the dependence of coherence with optical band, there are discrete sections that do show clear trends. Saliently, in the 1-5 Hz range, shorter wavelengths tend to be more coherent than longer ones (particularly in the epochs with the best statistics, such as 4 and 6) – this will be discussed in Section 4.3.4. There are also sections where the opposite is true – spikes in coherence at the QPO frequency in epochs 4 and 6 are stronger at longer wavelengths. These, again, will be noted in Section 4.4.

4.3.3 Phase lags

The phase lags can be seen in Fig. 7. Those in the range of 1-10 Hz are roughly the same across all observations, with a shift of $+\pi$ appearing at around 3 Hz; these reflect the presence and stability of the positively correlated peak. Above 10 Hz, there are few clear trends and it is difficult to make definitive claims; if this regime is dominated by components with <0.1-s delay, then we have many jumps from $+\pi$ to $-\pi$ over this period, and log binning would average out this behaviour.

However, one difference is the behaviour of the phase lags below 0.5 Hz. In epoch 1, the phase lags are mostly constant at $+ \pi/4$, and in epoch 2, they appear to increase towards lower frequencies. However, in epochs 3–5 (a month after outburst peak), phase lags change to roughly $\pm \pi$ – i.e. the two components are roughly in 'antiphase', where the peak of one component coincides with the trough of another (this is the Fourier representation of the anticorrelation component that appears in the CCF – see Fig. 3). The transition to this anticorrelation in the phase lags occurs at around 0.2 Hz, where there is a sudden discontinuity; analyses of epochs 4 and 5 are inconclusive in showing whether phase lags increase from $-\pi$ or decrease from $+\pi$ at this discontinuity. It is perhaps worth noting that negative phase lags, sometimes approaching $\pm \pi$, are seen at

lower frequencies in multiple other sources (see Gandhi et al. 2010; Veledina et al. 2017; Malzac et al. 2018; Vincentelli et al. 2021).

This lower frequency behaviour then changes again much later in the outburst during epoch 6, at which time the anticorrelation component is now bounded to a small section at roughly 0.3 Hz, with lower frequencies being generally above 0.

4.3.4 Time lags

The time lags can be seen in Fig. 8. At frequencies below ~ 0.2 Hz in epochs 3–5, there is confusion as to whether the time lags are positive or negative – this depends on whether the phase lags are assumed to be positive or negative, which is unclear from Fig. 7, as this is the point at which the phase lags are close to $\pm \pi$.

Fig. 8 also presents insets over the 1-10 Hz range, showing the similarities over the epochs. Shorter frequencies almost uniformly have a smaller lag than longer frequencies over this range; this is only not the case in epochs with poorer statistics (i.e. epoch 3) or below 2.5 Hz in epoch 6. This wavelength dependence will be discussed in Section 5.1, with epoch 6, in particular, discussed in Section 4.5.

4.4 Quasi-periodic oscillation – Its evolution and lags

In epochs 4–6, a feature can be seen that is similar to a QPO, with significant effects in the coherence and the lags. In epochs 4 and 5, this feature is at roughly 0.1 Hz, which increases to 0.3 Hz in epoch 6. Each bin with this feature shows (i) an increase in the power spectra, (ii) higher overall coherence (sometimes by an order of magnitude, particularly in epochs 4 and 6), (iii) greater coherence at longer wavelengths, (iv) small error bars in the lags, and (v) negative time lags (changing from -4 s in epoch 4 to -1 s in epoch 6). These features are best seen in epochs 4 and 6, where the statistics are better than other epochs.

This possible QPO can also be seen in the CCFs (Fig. 3). A positively correlated component can be seen between -4 and -3 s in epochs 3–5, and at -1 s in epoch 6, as indicated by the time lags seen in Fig. 8, often stronger at longer wavelengths. We briefly analysed the CCFs to test for the significance of this feature – see Section A1 in the Appendix.

As it turns out, a feature at this frequency is not a new discovery; Stiele & Kong (2020) showed the evolution of a QPO in X-rays over time that corresponds exactly with our feature described here. Therefore, there appears to be a connection with this QPO and the features, including a negative lag in the CCF, in our data. Indeed, QPOs have been associated with changes in the lags in other LMXB sources previously (Veledina et al. 2015; Malzac et al. 2018; Vincentelli et al. 2021).

Does this mean that the QPO shows optical variability preceding X-ray? Not necessarily; due to the periodic nature of phases (as discussed in Section 4.3.3), phase lags between π - 2π radians would be represented as negative lags between $-\pi$ -0, and this might be occurring here. Additionally, the negative lags seen in the CCF could just be a result of the periodic nature of this component; epochs 4 and 6, for example, show a second feature at positive lags (5 s and 2 s, respectively). These give a time period of 8 s and 3 s, respectively, between the two features; this matches the period of the QPO in both epochs (roughly 0.125 Hz and 0.3 Hz, respectively).⁵ See also

⁵We also see this behaviour in epoch 3, where we do not see clear similar QPO features. However, the QPO is still detected by Stiele & Kong (2020) during this time at a similar frequency. Additionally, with only 222 s of correlated

Section 4.5, where we simulate the Fourier components of epoch 6 and show how both the positive and negative correlations disappear when the QPO's Fourier components are removed. There is no clear mechanism by which a QPO would directly cause X-ray emission to lag optical emission in this way, while there are a number of models that would show the opposite (e.g. see Section 5.2); we thus consider the latter case to be the more likely one here.

4.5 The oddity of epoch 6

The QPO described in the previous section cannot, by itself, explain all the lags in epoch 6; the phase lags that are significantly different from other epochs extend over the frequency range of 0.08-2.5 Hz, not just around the QPO frequency. At these frequencies, shorter wavelengths have a consistently *greater* lag than longer wavelengths; this is the inverse trait of the sub-second lag seen between 1 and 5 Hz in other epochs (while this sub-second lag and wavelength dependence is still seen in epoch 6, note also how this new component supersedes it up to 2.5 Hz – Fig. 8).

The epoch 6 light curves show low coherence compared to other epochs (~0.01 – the only exception here is the 0.3-Hz frequency bin coincident with the QPO). As for the lags, over this range, g_s , r_s , i_s , and z_s bands even have *negative* lags with respect to X-rays, whereas u_s almost always has positive lags at the same frequency. This behaviour is also evident in the 2-s CCFs (Fig. 4), where the longer wavelength r_s , i_s , and z_s bands show a rising correlation at negative lags and peak at 0 s, while the shorter wavelength g_s band does not, and the u_s band shows an anticorrelation.

The QPO along with this different behaviour component are both strong features in epoch 6. To what magnitude, and in what ways, do they affect epoch 6's cross-correlation (Figs 3 and 4)? To find out, we simulated an approximation of the Fourier components of the X-rays and i_s band of epoch 6, creating a light curve for each from these components, and then cross-correlated them. We then modified the Fourier components to remove both the Lorentzian responsible for the QPO and the negative lags; for the latter, we instead assumed an interpolated flat distribution of $2\pi/5$ in the phase lags below 2 Hz. A CCF was made from these light curves as well, and the two results (as well as the inputs) are shown in Fig. 9.

Significantly, it can be seen how the cross-correlation is entirely different between -2 s and 3 s lags, no longer showing the negative correlations unique to epoch 6, nor the positive anticorrelation that is present in epochs 4 and 6. From this, we conclude that the QPO and the negative lags are the primary cause for the oddities we see in the epoch 6 CCF. For more information, including how each component affects the CCF individually and further evidence of the QPO influencing positive as well as negative lags, see Section A2 in the Appendix.

5 DISCUSSION

Analysis of our results has shown both features that are constant, and ones that are varying in specific ways over the course of the outburst. To summarize our main findings:

(i) In all epochs, J1820 shows rapid, sub-second red flares and longer scale variations that are stronger at longer wavelengths (Fig. 2).

time, epoch 3 has the poorest statistics of any of our epochs; this may explain why we do not see such QPO features.



Figure 9. Two simulations of the i_s band with X-rays from epoch 6. *Top*: Input Fourier components. The red lines are a representation of the data as it was seen in Figs 5–8, and the blue lines are a modification that removes the QPO and the negative lags from the i_s band's Fourier components between 0.02 and 2 Hz. *Bottom*: CCFs made by converting the Fourier components into light curves and then cross-correlating the results. CCFs were averaged over multiple 10-s segments. Note how the behaviour completely changes between -2 and +3 s, showing the significance of epoch 6's negative lags over this range.

(ii) Over the epochs, an anticorrelation component (stronger at longer wavelengths) around zero lag becomes increasingly significant – until late into the hard state decline, when it is superseded by a *positive* correlation at negative lags, again stronger at longer wavelengths (Fig. 3).

(iii) In all epochs, the CCF reveals a sub-second peak in the optical/X-ray correlation function at roughly 0.2 s. The peak maintains a roughly similar shape over the epochs but appears to shrink in comparison to other features (Fig. 4).

(iv) Over time, optical bands become less variable (i.e. decrease in power) at higher frequencies, but the variability/power remains roughly constant at lower frequencies. For X-rays, this relation is inverted, showing an overall decrease of rms² power at low frequencies. The optical power spectra also have consistently higher rms² power at longer wavelengths (Fig. 5).

(v) Coherence at lower frequencies drops as the outburst continues (Fig. 6).

(vi) The phase/time lags are mostly consistent between 1 and 10 Hz across epochs. At lower frequencies, they change from being near $\pm \pi/4$ to being near $\pm \pi$ as the outburst progresses. Epoch 6, however, fits neither of these trends (Fig. 7).

(vii) All epochs have an interval between Fourier frequencies of 1-5 Hz where shorter wavelengths have shorter time lags. This behaviour is roughly consistent (aside from in epoch 6), and neither the lag nor the separation by wavelength appears to change (Fig. 8).

In these observations lies evidence for evolving processes within the system. We will now address several key points and theories based on these observations.

5.1 Compact jet

Jet activity has already been found in this source (e.g. Homan et al. 2018; Bright et al. 2020), and the presence of rapid red variations and a sub-second optical lag that we show in this paper can both result from jet activity (Gandhi et al. 2017). Radio data (Bright et al. 2020) show the source to be relatively bright in the radio, and the long-term light curve approximates that in hard X-rays (Fig. 1). Meanwhile, Russell et al. (2018) presented evidence that the optical emission was likely on the optically thin tail of synchrotron power-law emission from a jet during 2018 April.

However, another interesting phenomenon ties in with this: the wavelength dependence of the sub-second optical lag. In Paice et al. (2019), we investigated the data shown in epoch 4, and it was first found that a component of the optical emission lagged the X-rays by roughly 170 ms. It was also found that this lag was dependent on wavelength; shorter wavelengths lagged less and longer wavelengths lagged more.

In the previous paper, it was suggested that this feature is emission from a compact jet. In this interpretation, we consider material emitting in hard X-rays close to the compact object from a jetemitting disc (Marcel et al. 2019; though it is also theorized that X-rays may come from the jet itself: Markoff, Nowak & Wilms 2005; Kylafis et al. 2008). A portion of this material is then ejected as a jet; with a fluctuating ejection rate, this does not necessarily lead to a uniform stream along the jet but instead an outflow that varies in density and/or Lorentz factor over time. We can interpret this as a series of discrete shells of matter; since these shells vary in speed, faster shells can thus collide with earlier, slower shells. When they do, they emit through synchrotron radiation. This is the internal shock model (Jamil, Fender & Kaiser 2010; Malzac 2013, 2014), the development of which has been motivated by research into gammaray bursts and active galactic nuclei jets (Rees & Meszaros 1994; Beloborodov 2000; Tchekhovskoy 2015). Tetarenko et al. (2021) found that the jet in this source is highly relativistic ($\Gamma = 6.81$); this would mean that a time delay of 170 ms corresponds to roughly 5×10^4 km between the X-ray and this synchrotron-emitting region.

The energy of this synchrotron emission is dependent upon the variation in the Lorentz factor of the colliding material; a larger gradient produces higher energy dissipation. Collisions between larger gradients also occur closer to the compact object and thus at shorter time lags. Since the regions close to the compact object are more compact, synchrotron emission from these regions is more self-absorbed and peaks at shorter wavelength. Thus, we see shorter time lags for shorter wavelength. A difference of 20 ms between z_s and u_s peak lags would, for a highly relativistic jet, correspond to a spatial extent of 6×10^3 km.

With the new observations presented in this paper, we have found that this behaviour is also not only present across *all* our epochs between 1 and 5 Hz in Fourier frequency but also appears to be fairly *consistent* in that range (with the exception of epoch 6, where a different component has the opposite effect on wavelengths up to 2 Hz) and is independent of the shape of the X-ray power spectrum.

However, while the behaviour stays more or less consistent, the relative contribution of this process to the overall variability appears to decrease over time; note the decreasing significance of the subsecond peak in Figs 3 and 4. We also note the significantly changing phase lags; Paice et al. (2019) suggested that $\pm \pi$ phase lags at low ($<\sim$ 1 Hz) frequencies could be a sign of Doppler boosting of a jet in high-inclination systems, which was put forward by Malzac et al. (2018). However, our analysis (see Fig. 7) now shows that $\pm \pi$ phase lags are not a constant feature of this source and appear only in the short time-scales covered by epochs 3–5. Additionally, the coherence also decreases over time as the lags change, similar to what has been seen in GX 339-4 (Vincentelli & Casella 2019, though note that this compares low hard-state and hard-intermediate-state observations).

Over this same range, the X-ray power spectra at these frequencies also decrease in strength over time, with a sharp decrease between epochs 1 and 2, where there is also a sharp decrease seen in the CCFs. Wijnands & van der Klis (1999) note that the Lorentzians that can describe the X-ray power spectra move to higher frequency over an outburst, which leads to such decreases in power at low frequencies. This is interpreted as resulting from changes in the source geometry.

What do we know of the evolution of the geometry of the source? Kara et al. (2019) found that the corona appears to shrink over the course of the hard state, based on a model that assumed a disc that extends to the ISCO. In our data, we see a broad anticorrelation, which is more often attributed to a hot flow inside a truncated disc (See Section 5.2). Zdziarski et al. (2021), meanwhile, describe a radially decreasing corona and also feature a truncated disc, inside which is a hot flow. In either scenario, an increasingly compact corona could mean that the X-ray emission from it would contribute less to variability at lower frequencies and would also correspond with a decrease in the significance of the jet component (because both the corona and the jet are linked through fluctuations in accretion power, which heat the X-ray-emitting corona and power the jet; thus, changes in one indicate changes in the other; Markoff et al. 2005). Overall, the corona becoming more compact would, by itself and its effect on the jet, explain several of features that we see.

The optical QPO could also be explained by a precessing jet. This geometrically based interpretation has the corona, which is connected to the jet, precessing in such a way that it creates variability in the light curves. This has been demonstrated in, e.g. Liska et al. (2018), though it is still a matter of debate (see e.g. Ingram & Motta 2020; Marcel & Neilsen 2021). The QPO may also contribute to the anticorrelation around zero lag in epochs 3–5; the high coherence at the QPO frequency would mean that smooth oscillations would be seen in the CCF, and the anticorrelation occurs between the QPO correlation peaks of -3 s and 5 s (also worth noting is that the QPO is stronger at longer wavelengths, a fact that is also true of the anticorrelation). It is thus feasible that the QPO contributes to the strength of the anticorrelation, though it need not necessarily be the sole cause of it (for instance, an anticorrelation at negative lags is

present in epochs 1 and 2, when no QPO could be seen in the optical power spectra).

5.2 Truncated disc and inner accretion flow

Is the disc truncated, and if so, does its inner radius evolve? Buisson et al. (2019) noted that, using relativistic reflection models, the inner edge of the accretion disc appears to remain steady and close to ISCO during most of the hard state; however, Zdziarski et al. (2021) noted the inner radius of the disc being much more truncated and evolving over time, moving inwards overall (though perhaps in a stochastic fashion). Likewise, De Marco et al. (2021) reported a truncated disc moving closer to the black hole as the hard state evolved.

If a disc's innermost radius is recessed from the black hole, then there is potential for a hot accretion flow to form. Both the observed fast UV/X-ray timing (Kajava et al. 2019) and the low optical polarization (Veledina et al. 2019) properties can be explained in terms of this (optically thin, geometrically thick) hot inner flow (Eardley, Lightman & Shapiro 1975; Ichimaru 1977; Narayan & Yi 1994).

Our observations show several features that could indicate this as a significant process. For instance, the CCFs in Fig. 3 show the presence of an anticorrelation in several of the epochs.

The anticorrelation can be expected if the hot flow broad-band spectrum has a pivoting point, e.g. if an increase of mass accretion rate leads to an increase in X-ray luminosity, at the same time causing higher synchrotron self-absorption within the flow (as a result of higher electron number density), thus leading to a drop in optical emission (Veledina, Poutanen & Vurm 2011). In this scenario, the variability amplitude is higher at energies further away from the pivoting point; hence, we expect to have stronger variability at longer wavelengths, as observed (Fig. 2).

In order to explain the complex anticorrelations at both positive and negative lags in epochs 4–6 in terms of the hot flow scenario, one needs to have two sources of both X-ray and optical emission (Veledina et al. 2017); X-rays would be produced by disc and synchrotron Comptonization and optical by synchrotron emission in the hot flow and irradiated disc emission. These features may appear in the spectrum close to the state transition. The natural expectation of such scenario is the different shape of the correlation with soft and hard X-rays, which we indeed see (more details in Section A3).

The presence of a simultaneous QPO at X-ray and optical wavelengths is another expectation of the hot flow scenario (Veledina, Poutanen & Ingram 2013b), which seems to be confirmed by our data from epochs 4 and 6. A correlated QPO can significantly alter the shape of the CCF (see e.g. Veledina et al. 2017) and can potentially explain some features of the epoch 6 CCF (see Section 4.5 and Fig. 9 for more discussion). On the other hand, the amplitude of phase lag at the QPO frequency, $\sim -\pi/2$, is not consistent with the expectation of the linear theory, which suggests either 0 or π depending on the system orientation (Veledina et al. 2013b; though it is worth noting that the QPO phase lag was closer to $\pm \pi$ at earlier epochs). Furthermore, the lag at the QPO frequency can be altered by the aperiodic component - however, quantitative conclusions on this possibility can be drawn only from dedicated simulations, which are beyond our present scope. Alternatively, if we assume that the true phase lag is positive (i.e. shifted by 2π), the reprocessing signal can contribute to the QPO (Veledina & Poutanen 2015): 0.3 Hz if within the range of frequencies at which the reprocessed QPO is not smeared out by the light travel delays.

The hot accretion flow scenario can explain most of the changing components in the CCF from different epochs but not the steady narrow peaks at sub-second lags. The fast optical correlation, most probably coming from a separate emission component, has to be added to the hot flow contribution to get the overall CCF shape consistent with the data.

5.3 Epoch 6 and the emergence of superhumps

Towards the end of the hard state, a superhump modulation at a period of ~ 0.7 d was first reported in the optical light curve of J1820 by Patterson et al. (2018) and then later expanded upon in Patterson (2019). This signal appeared around day 87 (MJD 58275), with post hoc analysis revealing that it may have appeared as early as MJD 58272. Epoch 6 took place on MJD 58276.2, very soon after the superhump appeared. Considering the times of maximum light noted in Patterson (2019), and assuming a period of 0.7 d, a maximum occurred at MJD 58276.23, essentially concurrent with epoch 6.

To date, there have been very few studies into the effect of superhumps on optical/X-ray correlations. Given that superhumps are considered to be a property of the outer disc (see Whitehurst & King 1991), the time-scales involved will correspond to the light travel time to the disc's tidal radius, which for J1820 will be ~ 10 s, and hence any correlated variations are likely to be heavily smeared, compared to the time-scales being studied here. Actually, optical/Xray CCFs were constructed for the black hole LMXB Swift J1753.5-0127 and were found to be independent of the superhump period present in that system (see section 3 of Durant et al. 2008, and note that 'orbital-like modulation' refers to superhumps). However, there have been no studies that examined phase lags in this scenario. Thus, this avenue of research would be valuable in investigating whether or not they contribute to the features we see in epoch 6 and, by extension, might be affecting the optical/X-ray correlations and variability of LMXB systems as a whole. Further studies of J1820's superhump properties can be found in Thomas et al. (2021; submitted).

5.4 A combined jet and hot flow model

Let us now link our findings to the various models presented. The source shows repeated rapid red flares and a sub-second optical/X-ray correlation that has a larger lag at longer wavelengths. The components dominating the correlation at low frequencies change as the hard state evolves; the X-ray power spectra and the optical/X-ray coherence both decrease at these frequencies, and the phase lags move towards $\pm \pi$. The source also becomes softer over time, and the sub-second lag in the cross-correlations becomes less significant. Meanwhile, the X-ray power and the coherence at higher frequencies remain static.

We do not find that the donor star is an explanation for our features; while the star could theoretically produce a correlated component at positive lags in our CCFs through X-ray heating and reprocessing, combining mass and orbital period estimates from Atri et al. (2020) and Torres et al. (2019) with Kepler's third law gives the distance between the compact object and donor to be ~ 16 light-seconds, and the effect in the lags would likely vary between epochs as we observe different phases, in disagreement with either the smooth evolution or the constant nature of the correlated components we see. However, given the high-system inclination ($\sim 75^{\circ}$, Torres et al. 2019), the shortest delays between X-ray and (reprocessed) optical photons from the near side of the disc are expected to be about ~ 0.5 s, with some additional smearing to longer lags due to light travel times across the face of the disc. Hence, it is possible that X-ray reprocessing off the accretion disc could be significant to the variability; this can be tested in future by comparing these results

to similar soft-state observations, where the illuminating component should be more dominant.

In all, we suggest a two-component model; one correlated, and the other anticorrelated. The correlated component we ascribe to a compact jet, which becomes less significant over time. The anticorrelated component, meanwhile, we ascribe to a hot flow, which remains static.

A jet as the correlated component would explain the red flares, the optical/X-ray sub-second correlation (Gandhi et al. 2017), and the larger lag at longer wavelengths (Malzac 2013, 2014). X-rays coming from the inflow would contribute more to the X-ray variability at the lowest (<0.1 Hz) and the highest (>1 Hz) frequencies. If the corona is contracting (evidenced either by a change in the vertical extent, as in Kara et al. 2019, or by a change in the radial extent and a decreasing disc truncation radius, as in Zdziarski et al. 2021), the variability of hard X-rays from that corona would decrease at lower frequencies, as would the optical/X-ray coherence over the same range – while the jet, closely linked to the corona, would also decrease in significance, leading to the decline of the sub-second correlation.

The latter, anticorrelated, component we ascribe to the hot flow. This component stays mostly static and thus, relatively, contributes more to the overall variability as the jet declines in significance. A hot flow scenario could feasibly also explain the QPO that we see in the data. The hot flow does not appear to increase in significance – note that the coherence does not increase.

5.4.1 Beyond the jet and hot flow

Muñoz-Darias et al. (2019) and Sánchez-Sierras & Muñoz-Darias (2020) reported the detection of optical and near-infrared winds, respectively, in J1820. The effect of winds on optical/X-ray timing correlations has not yet been explored in depth; however, they would occur on similar time-scales to those studied here. V404 Cyg is a similar system to J1820 (albeit with a much longer orbital period of 6.47 d and thus a larger physical scale; Casares, Charles & Naylor 1992); in that source, the wind-launching zone was found to be on the order of a few $\times 10^5$ km (Muñoz-Darias et al. 2016), or about 0.5 light-seconds. For a source inclination of 75° (Torres et al. 2019), and using equation (4) in Poutanen (2002), we get minimum lags on the order of 0.01 s, so contribution of the wind to the CCF time-scales that we probe is feasible from a timing standpoint.

However, the shallowness of the P Cygni absorption feature (1–2 per cent below the continuum level, Muñoz-Darias et al. 2019) implies that the wind is optically thin, which would mean that there would be minimal reprocessed emission due to the wind. Further investigation into this possibility would require better data on the optical depth and the ionization of the wind, combined with simulations.

6 CONCLUSIONS

We have presented analysis of optical and X-ray light curves from the black hole low-mass X-ray binary (LMXB) MAXI J1820+070 over the course of roughly 80 d. In doing so, we show an evolving cross-correlation function (CCF) at longer (\sim 10 s) time-scales, a consistent sub-second correlation, and various changes in the Fourier components, including differences between different optical wavelengths.

This paper thus shows both the dynamic and static nature of LMXBs, even over a single outburst. The shifting of phase lags at lower frequencies, the slowly climbing photon index, and the increasingly significant anticorrelation show how the coherent components

can change on a time-scale of weeks. Meanwhile, the constant nature of the correlation at sub-second lags, mid-frequency time lags, and rapid red flares in the light curves shows that other components are more stable and can be present with broadly static properties more than two months apart. Additionally, it shows how a QPO, travelling upwards through the Fourier frequencies, can change the resultant lags and correlation features.

We discuss our findings in terms of two synchrotron-emitting components – a correlated jet and an anticorrelated hot flow – as major contributors to the overall variability. If we allow for the jet to dominate at the lowest (<0.1 Hz) and the highest (>1 Hz) frequencies, and the hot flow to dominate in between, the interaction of these components can create the features we observe in several epochs.

A correlated component at negative lags can be seen in several epochs. Fourier analysis showed this component to be related to the frequency of a QPO in both the optical and X-ray light curves, previously reported in X-rays by Stiele & Kong (2020). The light curves are consistently coherent at these frequencies, with greater coherence (and thus correlation) at longer wavelengths. As the QPO increases in frequency over the outburst, the lag also evolves, becoming less negative. We note that, due to the periodic nature of the QPO, this negative lag could easily be a Fourier artefact, and the true lag is positive, with X-ray variability leading optical by several seconds.

Epoch 6 shows us features that are more difficult to understand. Between 0.08 and 2.5 Hz, there is some component that causes a drop in optical/X-ray phase lags. This component is more significant at longer wavelengths, and the lags become negative in most bands. The QPO mentioned earlier is in the middle of these frequencies, but there is no indication as to whether it is related or not. Further observations of LMXBs close to the intermediate state would be highly desirable to investigate this.

The evolution of the optical/X-ray correlations over the course of an LMXB's outburst remains an area rich with possibility for new discoveries. This paper highlights the fact that further, more frequent investigations of an LMXB over its hard state (and, ideally, over the transition to the soft state) would be invaluable in further decoding the shifting phenomena inside these sources.

ACKNOWLEDGEMENTS

We acknowledge support from Science and Technology Facilities Council (STFC) and a University Grants Commission - UK India Education & Research Initiative (UGC-UKIERI) Thematic Partnership. We would like to thank the anonymous referee for his or her helpful comments. We would also like to thank Joe Bright, Piergiorgio Casella, Rob Fender, Adam Ingram, Sera Markoff, Sara Motta, Tom Russell, Gregory Sivakoff, and Alex Tetarenko for their helpful conversations. We thank our ULTRACAM observers Paul Chote, Martin Dyer, and Anna Pala. We also thank Keith Gendreau, Zaven Arzoumanian, and the rest of the NICER team for their assistance in coordinating observations.

JAP is part supported by a University of Southampton Central VC Scholarship, and thanks D. Ashton for spectral timing help, as well as A. Stevens and D. Huppenkothen for help with the Stingray software.

TS thanks the Spanish Ministry of Economy and Competitiveness (MINECO; grant AYA2017-83216).

KR acknowledges funding from the European Research Council (ERC) under the European Union's Horizon 2020 research and innovation programme (grant agreement no. 694745).

AV acknowledges the Academy of Finland grant 309308 and the International Space Science Institute (ISSI) in Bern, Switzerland, for support.

This work was supported by the Programme National des Hautes Energies of Centre National de la Recherche Scientifique/Institut National des sciences de l'Univers (CNRS/INSU) with Institut de Physique (INP) and Institut National de Physique Nucleaire et de Physique des Particules (IN2P3), co-funded by Commissariat à l'énergie atomique et aux énergies alternatives (CEA) and Centre national d'études spatiales (CNES).

HiPERCAM and VSD were funded by the European Research Council (FP/2007-2013) under ERC-2013-ADG grant agreement no. 340040. ULTRACAM and VSD are funded by the STFC.

FMV acknowledges support from STFC under grant ST/R000638/1.

HiPERCAM observations were made with the Gran Telescopio Canarias (GTC) telescope (Spanish Observatorio del Roque de los Muchachos, Instituto de Astrofísica de Canarias), under Director's Discretionary Time. SMARTNet helped to coordinate observations. We have made use of software and web tools from the High Energy Astrophysics Science Archive Research Center (HEASARC) and made use of data and the 'Build XRT Products' tool supplied by the UK *Swift* Science Data Centre at the University of Leicester.

DATA AVAILABILITY

The NICER data underlying this article are available in the HEASARC Data Archive (https://heasarc.gsfc.nasa.gov/docs/archi ve.html). The ULTRACAM and HiPERCAM data will be shared on reasonable request to the corresponding author. The *Swift* data from Fig. 1 are available from the *Swift* Archive (https://www.swift.ac.u k/archive/). The AMI-LA data from Fig. 1 are available from Bright et al. (2020) (https://www.nature.com/articles/s41550-020-1023-5).

REFERENCES

- Adachi R. et al., 2020, Astron. Telegram, 13502, 1
- Atri P. et al., 2020, MNRAS, 493, L81
- Baglio M. C., Russell D. M., Lewis F., 2018, Astron. Telegram, 11418
- Bahramian A., Strader J., Dage K., 2018, Astron. Telegram, 11424, 1
- Belloni T., Hasinger G., 1990a, A&A, 227, L33
- Belloni T., Hasinger G., 1990b, A&A, 230, 103
- Beloborodov A. M., 2000, ApJ, 539, L25
- Bright J., Fender R., Motta S., 2018, Astron. Telegram, 11420
- Bright J. S. et al., 2020, Nature Astron., 4, 697
- Buisson D. J. K. et al., 2019, MNRAS, 490, 1350
- Casares J., Charles P. A., Naylor T., 1992, Nature, 355, 614
- Casella P. et al., 2010, MNRAS, 404, L21
- Corral-Santana J. M., Casares J., Muñoz-Darias T., Bauer F. E., Martínez-Pais I. G., Russell D. M., 2016, A&A, 587, A61
- De Marco B., Zdziarski A. A., Ponti G., Migliori G., Belloni T. M., Segovia Otero A., Dziełak M., Lai E. V., 2021, preprint (arXiv:2102.07811)
- Del Santo M., Segreto A., 2018, Astron. Telegram, 11427, 1
- Denisenko D., 2018, Astron. Telegram, 11400
- Dhillon V. S. et al., 2007, MNRAS, 378, 825
- Dhillon V. et al., 2018, Ground-based and Airborne Instrumentation for Astronomy VII, 10702, 157
- Done C., Gierliński M., Kubota A., 2007, A&A Rev., 15, 1
- Durant M., Gandhi P., Shahbaz T., Fabian A. P., Miller J., Dhillon V. S., Marsh T. R., 2008, ApJ, 682, L45
- Durant M. et al., 2011, MNRAS, 410, 2329
- Eardley D. M., Lightman A. P., Shapiro S. L., 1975, ApJ, 199, L153
- Eastman J., Siverd R., Gaudi B. S., 2010, PASP, 122, 935

- Evans P. A. et al., 2009, MNRAS, 397, 1177
- Fabian A. C. et al., 2020, MNRAS, 493, 5389
- Gaia Collaboration, 2020, A&A, 649, A1
- Gandhi P. et al., 2008, MNRAS, 390, L29
- Gandhi P. et al., 2010, MNRAS, 407, 2166
- Gandhi P. et al., 2016, MNRAS, 459, 554
- Gandhi P. et al., 2017, Nature Astron., 1, 859
- Gandhi P., Rao A., Johnson M. A. C., Paice J. A., Maccarone T. J., 2019, MNRAS, 485, 2642
- Gendreau K. C. et al., 2016, in den Herder J.-W. A., Takahashi T., Bautz M., eds, Proc. SPIE Conf. Ser. Vol. 9905, Space Telescopes and Instrumentation 2016: Ultraviolet to Gamma Ray, SPIE, USA, 99051H
- Hambsch J., Ulowetz J., Vanmunster T., Cejudo D., Patterson J., 2019, Astron. Telegram, 13014, 1
- Henden A. A., Levine S., Terrell D., Welch D. L., 2015, in American Astronomical Society Meeting Abstracts, Vol. 225. p. 336.16
- Homan J. et al., 2018, Astron. Telegram, 11576
- Huppenkothen D. et al., 2019, ApJ, 881, 39
- Ichimaru S., 1977, ApJ, 214, 840
- Imamura J. N., Steiman-Cameron T. Y., Middleditch J., 1987, ApJ, 314, L11
- Ingram A., Motta S., 2019, New Astronomy Reviews, 85, 101524
- Jamil O., Fender R. P., Kaiser C. R., 2010, MNRAS, 401, 394
- Kajava J. J. E., Motta S. E., Sanna A., Veledina A., Del Santo M., Segreto A., 2019, MNRAS, 488, L18
- Kanbach G., Straubmeier C., Spruit H. C., BelloniT., 2001, Nature, 414, 180
- Kara E. et al., 2019, Nature, 565, 198
- Kawamuro T. et al., 2018, Astron. Telegram, 11399, 1
- Kylafis N. D., Papadakis I. E., Reig P., Giannios D., Pooley G. G., 2008, A&A, 489, 481
- Lindegren L., 2020, A&A, 633, A1
- Liska M., Hesp C., Tchekhovskoy A., Ingram A., van der Klis M., Markoff S., 2018, MNRAS, 474, L81
- Littlefield C., 2018, Astron. Telegram, 11421, 1
- Magnier E. A. et al., 2020, ApJS, 251, 6
- Malzac J., 2013, MNRAS, 429, L20
- Malzac J., 2014, MNRAS, 443, 299
- Malzac J. et al., 2018, MNRAS, 480, 2054
- Marcel G., Neilsen J., 2021, ApJ, 906, 106
- Marcel G. et al., 2019, A&A, 626, A115
- Markoff S., Nowak M. A., Wilms J., 2005, ApJ, 635, 1203
- Mereminskiy I. A., Grebenev S. A., Molkov S. V., Zaznobin I. A., Khorunzhev G. A., Burenin R. A., Eselevich M. V., 2018, Astron. Telegram, 11488, 1
- Motch C., Ilovaisky S. A., Chevalier C., 1982, A&A, 109, L1
- Motch C., Ricketts M. J., Page C. G., Ilovaisky S. A., Chevalier C., 1983, A&A, 119, 171
- Muñoz-Darias T. et al., 2016, Nature, 534, 75
- Muñoz-Darias T. et al., 2019, ApJ, 879, L4
- Mushotzky R. F., Done C., Pounds K. A., 1993, ARA&A, 31, 717
- Narayan R., Yi I., 1994, ApJ, 428, L13
- Negoro H. et al., 2018, Astron. Telegram, 12057, 1
- Pahari M., Gandhi P., Charles P. A., Kotze M. M., Altamirano D., Misra R., 2017, MNRAS, 469, 193
- Paice J. A., GandhiP., Page K., Altamirano D., Court J., CharlesP., 2018, Astron. Telegram, 11432, 1
- Paice J. A. et al., 2019, MNRAS, 490, L62
- Patterson J., 2019, Buchheim R. K., et al., eds, Proc. 38th Annual Conf. Society for Astronomical Sciences, (Rancho Cucamonga, CA: Society for Astronomical Sciences). p. 61, http://www.socastrosci.org/Publicatio ns.html
- Patterson J. et al., 2018, Astron. Telegram, 11756, 1
- Poutanen J., 2002, MNRAS, 332, 257
- Rees M. J., Meszaros P., 1994, ApJ, 430, L93
- Russell D. M. et al., 2018, Astron. Telegram, 11533, 1
- Sako S., Ohsawa R., Ichiki M., Maehara H., Morii M., Tanaka M., 2018, Astron. Telegram, 11426, 1
- Sánchez-Sierras J., Muñoz-Darias T., 2020, A&A, 640, L3

Shidatsu M., Nakahira S., Murata K. L., Adachi R., KawaiN., Ueda Y., Negoro H., 2019, ApJ, 874, 183

- Stiele H., Kong A. K. H., 2020, ApJ, 889, 142
- Tchekhovskoy A., 2015, Launching of Active Galactic Nuclei Jets. Springer, Switzerland, p. 45,
- Tetarenko A. J. et al., 2021, MNRAS,
- Timmer J., Koenig M., 1995, A&A, 300, 707
- Tomsick J. A., Homan J., 2019, Astron. Telegram, 12732, 1
- Torres M. A. P., Casares J., Jiménez-Ibarra F., Muñoz-Darias T., Armas Padilla M., Jonker P. G., Heida M., 2019, ApJ, 882, L21
- Tucker M. A. et al., 2018, ApJ, 867, L9
- Ulowetz J., Myers G., Patterson J., 2019, Astron. Telegram, 12567, 1
- Uttley P. et al., 2018, Astron. Telegram, 11423, 1
- van der Klis M., 2000, ARA&A, 38, 717
- Vaughan B. A., Nowak M. A., 1997, ApJ, 474, L43
- Veledina A., 2016, ApJ, 832, 181
- Veledina A., 2018, MNRAS, 481, 4236
- Veledina A., Poutanen J., 2015, MNRAS, 448, 939 Veledina A., Poutanen J., Vurm I., 2011, ApJ, 737, L17
- Veledina A., Poutanen J., Vurm I., 2011, ApJ, 757, E17 Veledina A., Poutanen J., Vurm I., 2013a, MNRAS, 430, 3196
- Veledina A., Poutanen J., Ingram A., 2013b, ApJ, 778, 165
- Veledina A., Revnivtsev M. G., Durant M., Gandhi P., Poutanen J., 2015, MNRAS, 454, 2855
- Veledina A., Gandhi P., Hynes R., Kajava J. J. E., Tsygankov S. S., Revnivtsev M. G., Durant M., Poutanen J., 2017, MNRAS, 470, 48
- Veledina et al., 2019, A&A, 623, A75
- Venables W. N., Ripley B. D., 2002, Modern Applied Statistics with S, 4th edn. Springer, Switzerland, doi:10.1007/978-0-387-21706-2
- Vincentelli F. M., Casella P., 2019, Astron. Nachr., 340, 319
- Vincentelli F. M. et al., 2021, MNRAS, 503, 614
- Whitehurst R., King A., 1991, MNRAS, 249, 25
- Wijnands R., van der Klis M., 1999, ApJ, 514, 939
- Xu Y., Harrison F., Tomsick J., 2019, Astron. Telegram, 13025, 1
- Yu W., Zhang J., Yan Z., Wang X., Bai J., 2018, Astron. Telegram, 11510, 1
- Zampieri L., Munari U., Ochner P., Manzini F., 2019, Astron. Telegram, 12747, 1
- Zdziarski A. A., Dzielak M. A., De Marco B., Szanecki M., Niedzwiecki A., 2021, Astrophys. J. Lett., 909, L9

APPENDIX A: APPENDIX

A1 CCF significance test

First, we analysed the significance of our CCFs. We simulated light curves based on our optical data, uncorrelated with X-rays, and then ran CCFs on those. To do this, we Fourier transformed the light curves, randomized the phases (i.e. the arguments of the resulting complex numbers), and then inverse Fourier transformed the result (using methodology laid out in Timmer & Koenig 1995). This simulated light curve therefore had the same power spectrum as the source light curve but was randomized in time and would thus be uncorrelated with respect to X-rays.

This was done 1000 times. Each time, the simulated, uncorrelated light curve was cross-correlated with the X-rays, and the resultant CCF was recorded. At the end, for each lag bin, the 5–95 per cent intervals of all simulations were found. We used this as a way of measuring the significance of features in the original CCF; any features that lie outside of these intervals are considered to be significant. The negative lag feature was found to be outside these intervals for epochs 3–6, and thus we consider it to be a significant feature rather than a spurious result (Fig. A1).



Figure A1. The g_s band versus X-ray CCF from epoch 4, averaged over 162 segments 10 s in size, is shown in green – similar to that seen in Fig. 3, but without binning. A representative error bar is plotted. The faded grey area is 1000 overlapping simulated correlation functions, and the black dotted lines are the 5 per cent and 95 per cent intervals of all the simulations. The feature at -3 s, noted in Section 4.4, is above this significance line. The -1-s feature in epoch 6 was similarly found to be significant.

A2 Simulated Fourier components

As part of our analysis, we wanted to investigate what correlations we would see if we modified certain variability features of the source. We did this by using a custom code that simulated Fourier features and inputted features akin to those seen in Figs 5–8. The code created light curves out of these features and then carrying out cross-correlation analysis on those resultant light curves. The majority of the analysis on the simulated light curves was carried out by the Stingray⁶ PYTHON package (Huppenkothen et al. 2019).

We were thus able to modify the light curves by changing the Fourier features. Fig. 9 shows two variants: a simulation meant to reproduce the epoch 6 features (red) and one that removes all negative-lag trends and the QPO between 0.02 and 2 Hz. Fig. A2 shows two more variants intended to clarify the contributions of these components – namely, a version that just removes the QPO (green) and a version that just removes the negative-lag trends (gold).

The synthetic CCFs here reveal which features are due to which Fourier components. The +0.5-s anticorrelation and the +2-s correlation, for example, are primarily due to the QPO, while the -1-s correlation is mainly due to the negative lags. In both, a sub-second lag is still present, showing that it is independent of the variability below 2 Hz.

A3 Additional epoch 6 CCFs

We studied the dependence of the CCF shape on the X-ray energy band for epoch 6. We considered two ranges: 0.1–1.0 keV and 3.0– 12.0 keV. The resulting CCFs are shown in Fig. A3. The correlations look significantly different in soft and hard X-rays, while the optical/soft-X-ray CCF is dominated by the peak at small negative lags, and the shape of the optical/hard X-ray CCF more resembles a sinusoid. Interestingly, the narrow peak at positive lags, which we attribute to the jet, is more prominent in the soft CCF, though it is present in both at the same lag.

Previous studies of the dependence of CCF shape on the X-ray energy band have been performed for Swift J1753.5–0127 (Durant

⁶https://github.com/StingraySoftware/stingray



Figure A2. A further two simulations of the i_s band with X-rays from epoch 6. *Top*: Input Fourier components. The green lines are a modification of the behaviour of epoch 6 with the QPO removed, and the gold lines are a modification that removes the negative lags. *Bottom*: CCFs made by converting the Fourier components into light curves and then cross-correlating the results. CCFs were averaged over multiple 10-s segments. Note how each change affects the CCF in different waves; specifically, the presence of an anticorrelation at -2 s and a correlation at +3 s.

et al. 2008; Durant et al. 2011), GX 339–4, and the neutron star binaries Sco X-1 and Cyg X-2 (Durant et al. 2011). These show shape variations, yet such acute difference of CCF shape seen in this paper has never been reported before.

The difference may appear due to presence of two separate components in the X-ray band, e.g. softer component coming from Comptonization of disc photons and harder component coming from hot flow synchrotron Comptonization (Veledina 2016). Recent spectral studies indeed suggest the presence of two Comptonization continua (Zdziarski et al. 2021). The variability of both of these is caused by the propagating fluctuations; however, their



Figure A3. Two additional CCFs from epoch 6, made from 10-s segments. The CCFs are optical bands versus soft X-rays (0.1–1.0 keV, *Top*) and versus hard X-rays (3.0–12.0 keV, *Bottom*).



Figure A4. Phase lags from epoch 4, in the u_s band only, rebinned to best show these variations. The red box indicates a region where there might be a sinusoidal variation.

response may alter between harder-when-brighter behaviour for the synchrotron Comptonization to softer-when-brighter behaviour for the disc Comptonization, resulting in a complex variability pattern (Veledina 2018). Correlation with the optical components (disc, jet, and hot flow) is naturally expected to be different for these X-ray components, leading to difference between X-ray energy bands, as the fraction of synchrotron- to disc-Comptonization depends on the energy. The weighted average of the sharply different soft and hard CCFs may then lead to the complex CCF shape seen in Fig. 3.

A4 Possibility of a flared disc

The phase lags for epoch 4 appear to show peaks in the range of 0.1-5 Hz (see Fig. A4). Such features have previously been proposed to originate in a highly flared disc (Poutanen 2002 – see Fig. 6 within). In this model, these peaks can result from features in the power density spectrum and reflection from the outer disc.

To investigate, we rebinned the data until they best showed this feature. Then, two models were fit to the phase lags over this range,

the first being a line, and the second being a line with a sinusoid added on top, both in linear space. However, the second model was not found to fit the phase lags significantly better than the first. There was ambiguity in the results; relative to the variations in the phase lags themselves, large errors are present that allowed for both models to be viable. Hence, while we do not consider the peaks in epoch 4 to be evidence for a flared disc, we note that this could be a topic for further investigation in future observations of J1820.

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