

LETTER TO THE EDITOR

Using LSST late-time photometry to constrain Type Ibc supernovae and their progenitors

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ABSTRACT

Over its lifespan, the *Vera C. Rubin* Observatory Legacy Survey of Space and Time (LSST) will monitor millions of supernovae (SNe) from explosion to oblivion, yielding an unprecedented *^u*g*rizy* photometric dataset based on their late-time evolution. Here, we show that the photometric evolution of Type Ibc SNe can be used to constrain numerous properties of their ejecta, without the need for expensive spectroscopic observations. Using radiative-transfer simulations for explosions of He-star progenitors of different initial masses, we show that the g-band filter primarily follows the strength of the Fe II emission, the r-band [O I] $\lambda\lambda$ 6300, 6364 and [N II] $\lambda\lambda$ 6548, 6583, the *i*-band [Ca II] $\lambda\lambda$ 7291, 7323, and the *z*-band the Ca II $\lambda\lambda$ 8498 − 8662 triplet, hence providing information on nucleosynthetic yields. Information on weaker lines that may be used, for example, to constrain clumping is absent. However, this deficiency may eventually be resolved by improving the physical realism of radiative-transfer simulations through a closer connection to physically consistent 3D explosion models, as well as through the judicial selection of a much smaller set of spectral observations. Degeneracies inherent to the SN radiation will affect the interpretation of photometric measures, but line fluxes from nebular-phase spectra are similarly compromised. Importantly, our "family" of Type Ibc SN models follows a distinct trajectory in color-color magnitude diagrams as the ejecta evolve from 100 to 450 d, allowing for the disentanglement of different progenitors or explosions. This photometric procedure provides a promising approach to studying statistical samples of SNe Ibc and confronting them with consistently improving progenitor and explosion models, as well as capturing the onset of late-time interaction with circumstellar material or identifying events currently unknown.

Key words. supernovae: general – radiative transfer – line: formation

1. Introduction

The supernova (SN) community is approaching an important turning point following decades of discovery with regard to massive star explosions, growing from a few per year to many each night (see, e.g., [Sullivan](#page-4-0) [2013\)](#page-4-0) thanks to numerous all-sky surveys such as PTF [\(Law et al.](#page-4-1) [2009\)](#page-4-1), Pan-STARRS [\(Kaiser et al.](#page-4-2) [2010\)](#page-4-2), ASAS-SN [\(Shappee et al.](#page-4-3) [2014\)](#page-4-3), and ATLAS [\(Tonry et al.](#page-4-4) [2018\)](#page-4-4). In parallel, the modeling of SN radiation has been expanded considerably, with the development of numerous tools to model light curves and spectra. However, much of this modeling has focused on only a few well-observed nearby events. In addition, due to obvious observational challenges, these studies are also biased in favor of the high brightness, photospheric phase rather than the low-brightness, ever-dimming nebular phase.

With the *Vera C. Rubin* Observatory Legacy Survey of Space and Time (LSST; [LSST Science Collaboration](#page-4-5) [2009\)](#page-4-5), the SN discovery rate will be further enhanced. To maximize the use of this treasure-trove of data there is an urgent need to develop photometric techniques that can constrain SN properties and be used to provide constraints on stellar and galactic evolution, as is currently undertaken based on spectroscopy. Photometry is less time-consuming than spectroscopy and it can be obtained for fainter objects, along with the fact that it is gathered in a systematic manner with modern, untargeted sky surveys. Furthermore,

the very faint magnitude detection limit allows for a monitoring of SNe out to very late times. A continuous photometric light curve of SNe can thus be built from maximum light until late times, yielding information that is competitive over that obtained using spectra, which are much harder to obtain and which have a much poorer temporal coverage.

The LSST will yield an unprecedented number of SNe suitable for statistical analyses, with estimates of ∼ 3.3 million Type II SNe and 580 thousand Type Ibc SNe for a ten year survey. Within a redshift of 0.07, the total would be about 25 thousand Type II SNe and about eight thousand Type Ibc SNe. About 4400/4300/3000 of such SNe Ibc will have LSST photometric detections in g/g*r*/g*ri* at 100 days after maximum light. At 200 d, these numbers change to 2300/2000/1700 and at 300 d, they are 400/380/380. These estimates come from the Photometric LSST Astronomical Time Series Classification Challenge (PLAsTiCC; [Kessler et al.](#page-4-6) [2019;](#page-4-6) [Hložek et al.](#page-4-7) [2020\)](#page-4-7) and are based at nebular times on the theoretical light curves of Dessart et al. (in prep.)^{[1](#page-0-6)}. In the absence of dust (and molecule emission), the coverage from ∼3600 (*u* band) to ∼9700 Å (*y* band) captures typically

ZTF obtains g and r band photometry down to 20–20.5 mag and therefore captures a subset of what LSST will provide in terms of depth and spectral coverage. Similarly, Pan-STARRS obtains g*rizy* photometry down to ∼21 mag, and thus does not go as deep as the LSST.

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70% of the SN light at nebular times and, thus, permits the determination of the bolometric luminosity, although reddening and distance (redshift) may not be trivial with regard to obtaining accurate estimates. Corrections for host contamination are also easier and more robustly done with difference imaging and photometry, as compared to typical slit spectroscopy.

During the photospheric phase, the bolometric luminosity, the brightness in various photometric filters, and the colors provide constraints on the progenitor radius and the global properties of the ejecta such as its mass and kinetic energy. However, these only provide limited information on the composition with the exception of ⁵⁶Ni (i.e., in ejecta where its decay provides the main energy source for the SN luminosity). In contrast, at nebular times, the ejecta is relatively optically thin, and the SN radiation is primarily seen as line emission. This is particularly evident in Type Ib (and IIb) and Ic SNe at about a year post-explosion when most of the optical flux is contained in [O I] $\lambda\lambda$ 6300, 6364, and [Ca II] $\lambda\lambda$ 7291, 7323.

Omitting the line profile morphology, the photometry yields very similar information to spectroscopy at late times – the relative strength of important emission lines may be inferred from a well-chosen optical color. For example, the *r* − *i* color contains essentially the same information as the flux ratio of the [O I] $\lambda\lambda$ 6300, 6364 and [Ca II] $\lambda\lambda$ 7291, 7323 lines (modulo the contribution of the [N II] $\lambda\lambda$ 6548, 6583 line in the lower mass models; Fig. [A.1\)](#page-5-0). With radiative transfer modeling, it is possible to constrain the mass of the elements associated with this line emission [\(Fransson & Chevalier](#page-4-8) [1989\)](#page-4-8). Although this has been done so far exclusively using the detailed information in spectra, the LSST motivates the use of photometric measures alone to deliver similar constraints on the ejecta nucleosynthesis. With the large number of SNe that will be monitored for years by the LSST, such a photometric approach may be applied to a statistical sample of SNe, constraining some properties of the ejecta and progenitor, as well as connecting these to the host populations that will also be resolved in finer detail than ever before (by the LSST itself, as well as with the next generation large telescopes; see, e.g., [Galbany et al.](#page-4-9) [2018;](#page-4-9) [Kuncarayakti et al.](#page-4-10) [2018\)](#page-4-10).

In the next section, we illustrate how photometry, and in particular colors, can be used to assess the relative strength of line emission in SNe Ibc at nebular times, allowing for the identification of different types of ejecta composition based on photometry alone. In Sect. [3,](#page-3-0) we discuss the limitation of this method and possible workarounds for these. In Sect. [4,](#page-4-11) we present our conclusions.

2. Colors as a proxy for line-flux ratios

Figure [1](#page-1-0) shows the *^u*g*riz* LSST filters together with a nebular spectrum for a SN ejecta arising from the explosion of a star that started on the He zero age main sequence (ZAMS) with a mass of $6 M_{\odot}$ [\(Dessart et al.](#page-4-12) [2021a;](#page-4-12) hereafter D21; this model would most likely have been classified as a SN Ib; [Dessart et al.](#page-4-13) [2020\)](#page-4-13). This spectrum is dominated by lines of moderate to large strength such as Mg_I] λ 4571, Na_I λ λ 5896, 5890, [O_I] λ λ 6300, 6364, [N ii] λλ ⁶⁵⁴⁸, 6583, [Ca ii] λλ ⁷²⁹¹, 7323, O ⁱ λλ ⁷⁷⁷¹ [−] 7775, and Ca II $\lambda\lambda$ 8498−8662, together with many weak Fe II lines contributing a moderate but extended background emission between 4000 and 5500 Å. In some models characterized by low ionization, Fe recombines, and the Fe II emission in the blue disappears in favor of Fe I emission further to the red $(D21)$.

The emission from low-redshift Type Ibc SNe ($z \le 0.07$) is captured in a "convenient way" by the LSST photometric filters since the landmarks of their nebular spectra fall in dis-

Fig. 1. Spectrum for model he6p0 at 428 d after explosion (thick black line; Dessart et al., in prep.) together with the normalized LSST *^u*g*riz* filter transmission functions (the *y* filter is not included in that figure). The thin black line is the model spectrum for a redshift of 0.2. For redshifts of ∼0.1 the photometric measures would be hard to use since [O I] $\lambda\lambda$ 6300, 6364, and [Ca II] $\lambda\lambda$ 7291, 7323 fall between filters.

tinct filters. The strong Fe II emission, which arises from the Herich shell at all times or from the O-rich shell at early times, falls in the q band. [O_I] $\lambda\lambda$ 6300, 6364 falls in the r band, together with weaker contributions from Fe II lines early on and by [N II] $\lambda\lambda$ 6548, 6583 later on in progenitors that retained their He/N shell all the way to core collapse. [Ca II] $\lambda\lambda$ 7291, 7323 falls in the *i* band and dominates over other contributions from Fe II or Ni II, while Ca II $\lambda \lambda$ 8498 – 8662 falls in the *z* band. Finally, we mention the *u* band which will provide insights into the possible interaction of the ejecta with circumstellar material (CSM). In Type II SNe, $H\alpha$ is always strong and falls in the same filter as [O I] $\lambda\lambda$ 6300, 6364 so the [O I] line flux contribution to the *r*-band magnitude cannot easily be made in H-rich ejecta with such photometric filters. Type II SNe are thus not included in the following discussion.

What is of particular interest here is whether it is possible to constrain the progenitors and yields of Type Ibc SNe based on photometry alone. In other words, we consider whether photometry alone distinguish robustly progenitors that died with different abundances of O, He, or N. Practically, this requires that differences in line fluxes seen in explosion models of different ages, compositions, or energetics correspond to clear differences in photometric properties. Degeneracies that lead to similar line fluxes or line flux ratios from distinct models will impact both photometric and spectroscopic measures – this issue concerns the physics of SN ejecta and the degeneracy of the SN radiation itself. Extensive time coverage that is available with photometry may help to break some of these degeneracies.

To test the usefulness of photometry, Dessart et al. (in prep.) employed the He-star explosion simulations of [D21](#page-4-12) and evolved these from an earlier time of 100 d (rather than 200 d) to about 450 d after explosion with the nonlocal thermodynamic equilibrium time-dependent radiative transfer code CMFGEN [\(Hillier & Dessart](#page-4-14) [2012\)](#page-4-14). The sample of models includes initial He-star masses of 2.6, 2.9, 3.3, 3.5, 4.0, 4.5, 5.0, 6.0, 7.0, 8.0, and $12.0 M_{\odot}$ (the models are named he2p6 etc.; see Table [1,](#page-2-0) [Woosley](#page-4-15) [2019,](#page-4-15) and [Ertl et al.](#page-4-16) [2020\)](#page-4-16). An extensive description of the resulting spectra and ejecta properties is deferred to a forthcoming study (Dessart et al., in prep.) but since it can help understand what drives the photometric changes, we show the spectral evolution for a low-mass and a high-mass He-star model in Fig. [A.2.](#page-5-1) Here, we focus on their photometric properties and we selected only a subset of representative models, namely he2p6, he4p0, he5p0, he6p0, he8p0, and he12p0. The [D21](#page-4-12) models with clumping throughout the ejecta or only in the O-shell are excluded for conciseness.

Table 1. Ejecta properties of our set of Type Ibc models from [D21.](#page-4-12)

Model	M_{ZAMS} $[M_{\odot}]$	M_{presN} $[M_{\odot}]$	$M_{\rm ei}$ $[M_{\odot}]$	$E_{\rm kin}$ [foe]	4^4 He $[M_{\odot}]$	16 O $[M_{\odot}]$	${}^{56}Ni_{t=0}$ $[M_{\odot}]$
he2p6	13.85	2.15	0.79	0.13	0.71		$2.28(-2)$ 1.22(-2)
he2p9	14.82	2.37	0.93	0.37	0.77		$5.03(-2)$ $2.32(-2)$
he3p3	16.07	2.67	1.20	0.55	0.84		$1.51(-1)$ $4.00(-2)$
he3p5	16.67	2.81	1.27	0.41	0.87		$1.72(-1)$ $2.92(-2)$
he4p0	18.11	3.16	1.62	0.63	0.92		$3.10(-1)$ $4.45(-2)$
he4p5	19.50	3.49	1.89	1.17	0.95		$4.19(-1)$ $8.59(-2)$
he5p0	20.82	3.81	2.21	1.51	0.97	$5.92(-1)$	$9.77(-2)$
he6p0	23.33	4.44	2.82	1.10	0.95	$9.74(-1)$	$7.04(-2)$
he7p0	25.68	5.04	3.33	1.38	0.90	1.29(0)	$1.02(-1)$
he8p0	27.91	5.63	3.95	0.71	0.84	1.71(0)	$5.46(-2)$
he12p0	35.74	7.24	5.32	0.81	0.23	3.03(0)	$7.90(-2)$

Notes. The table columns correspond to the ZAMS mass, the preSN mass, the ejecta mass, the ejecta kinetic energy (1 foe $\equiv 10^{51}$ erg), and the cumulative yields of 4 He, 16 O, and 56 Ni prior to decay (see discussion in [D21\)](#page-4-12). Numbers in parentheses represent powers of ten.

Fig. 2. Photometric properties of a sample of He-star explosion models from 100 to about 450 d after explosion. The bolometric light curve is shown at top, followed by the color curves $q - r$, $r - i$, and $r - z$. The original models are presented in $D21$, but their full time evolution is discussed in Dessart et al. (in prep.).

Some photometric properties of our models are shown in Fig. [2.](#page-2-1) Because the kinetic energy tends to increase with ejecta mass, the fading rate is similar between models. The decay power varies by about a factor of ten (the initial ⁵⁶Ni mass covers the range 0.01 up to 0.1 M_{\odot}), while in all models the fraction of γ rays that escape increases by a factor of about five between 100 and 450 d. Hence, the bolometric light curves appear ordered in mass and do not cross as time passes. When considering photometry, and especially observations, the magnitude in a given band will depend on, for example, the 56 Ni mass, and the distance, reddening, and redshift of the SN. In contrast, working with colors directly takes out the issue with distance, and takes out some of the influence of variations in ⁵⁶Ni mass. So, color is a more direct way to distinguish the models.

The bottom three panels of Fig. [2](#page-2-1) illustrate the color evolution in $g - r$, $r - i$, and $r - z$. The g-band brightness primarily

Fig. 3. LSST color-color magnitude diagram for the Type Ibc simulations of Dessart et al. (in prep.) from 100 to about 450 d after explosion. We show the color curves *^r*−*ⁱ* vs. g−*^r* for our He-star explosion models from 100 d (indicated by a star symbol) until the end of the simulation at around 450 d. Dots are equally spaced in time every 20 d. The arrow corresponds to the color shift caused by $A_V = 1$ mag.

reflects the strength of Fe II emission, with a growing contribution from Mg I] λ 4571 at late times. [D21](#page-4-12) found that this Fe II emission is relatively strong in the lower mass He-star models, since Fe II is the primary coolant for the He-rich shell (which represents 90% of the ejecta mass in model he2p6) or for the O-rich shell when O is partially ionized (model he5p0 here). The *r* band contains [O I] $\lambda\lambda$ 6300, 6364, [N II] $\lambda\lambda$ 6548, 6583, as well as Fe II line emission. The latter is strong around 100 d and weakens in time. In contrast, $[N II] \lambda \lambda$ 6548, 6583 ([O I] $\lambda\lambda$ 6300, 6364) is strengthened continuously from 100 to 450 d in models with a massive He-rich (O-rich) shell. Models of greater mass, or of lower expansion rate, tend to be more recombined and thus lie at higher g [−] *^r* values (redder color).

The *i* band is mostly sensitive to $\left[\text{Ca II} \right] \lambda \lambda$ 7291, 7323, which forms in the Fe/He and Si/S shells of the ejecta [\(Jerkstrand et al.](#page-4-17) [2015;](#page-4-17) [D21\)](#page-4-12)^{[2](#page-2-2)}. The slowly growing $r - i$ color indicates a progressive though modest strengthening of [Ca II] $\lambda\lambda$ 7291, 7323 relative to [O I] $\lambda\lambda$ 6300, 6364. In models with a He-rich shell, [N II] $\lambda\lambda$ 6548, 6583 becomes very strong at late times and drives $r - i$ to negative values. This effect is very strong in model he2p6, so much so that one could mistake [N II] $\lambda\lambda$ 6548, 6583 with H α , as observed in SN 1993J [\(Matheson et al.](#page-4-18) [2000\)](#page-4-18). Finally, the *z* band is a good tracer of Ca II $\lambda\lambda$ 8498 – 8662. In lower mass He-star models, this triplet is weak because Ca is overionized through most of the ejecta (i.e., the He-rich shell). In higher mass models, Ca II $\lambda \lambda$ 8498 − 8662 forms in the O-rich shell and is strong at earlier times when the ejecta is not too optically thin. In all cases, the [Ca II] $\lambda\lambda$ 7291, 7323 is stronger at late times (for an additional discussion and details, see [D21](#page-4-12) and Dessart et al., in prep.).

A more direct way to distinguish the models shown in Fig. [2](#page-2-1) is to consider the color–color magnitude diagram, $r - i$ vs. $q - r$

² In contrast to [Li & McCray](#page-4-19) [\(1993\)](#page-4-19), [Dessart et al.](#page-4-20) [\(2021b\)](#page-4-20) find that [Ca II] $\lambda\lambda$ 7291, 7323 also forms in the Fe/He and Si/S shells in Type II SN ejecta.

(Fig. [3\)](#page-2-3). Not only do the models lie in different parts of the diagram, but the trajectories they follow as they evolve are distinct. Lower mass models lie at small (negative) $q - r$ values, only moving to the right at late times, preferentially at small (negative) $r - i$ values because of the strong flux in the *r* band due to [O I] $\lambda\lambda$ 6300, 6364 or [N II] $\lambda\lambda$ 6548, 6583. Higher mass models, with a greater O yield, are systematically redder and lie at higher $q - r$ values, with a small $r - i$ value that reflects the dominance of [O I] $\lambda\lambda$ 6300, 6364 over the optical spectrum. These photometric properties are based on a subset of the Hestar explosion models of [D21,](#page-4-12) which have their own idiosyncrasies. The present set of trajectories is primarily illustrative but it shows that this color-color magnitude diagram captures the basic spectral families drawn out by these models – the photometry conveys rich information that is similar to that offered by the spectra.

Even today, it is still a struggle to obtain a well-sampled spectral evolution at nebular times. Often, the spectra are truncated in the blue or in the red, so that $\left[$ Ca II $\right]$ $\lambda \lambda$ 7291, 7323 (and especially Ca II $\lambda \lambda$ 8498 − 8662) may not be observed. Many observations are stopped at around 300 d and the coverage up to that phase is often sparse. Spectra are often noisy in dis-tant objects, especially at later times. Figure [4](#page-3-1) shows the $r - i$ color evolution for a few SNe Ib and Ic, together with the small model set used here. Here, the photometry is computed from the spectra by convolution with the LSST filters, which was a challenge for the reasons given above. Nonetheless, Fig. [4](#page-3-1) confirms that the relative strength of [O I] $\lambda\lambda$ 6300, 6364 and [Ca II] $\lambda \lambda$ 7291, 7[3](#page-3-2)23 is captured with photometry alone³. In the future the goal is to complement figures similar to Figs. 3 and 4 future, the goal is to complement figures similar to Figs. [3](#page-2-3) and [4](#page-3-1) with a larger set of improved progenitor and explosion models, including the SNe Ibc monitored by LSST, as well as explore the results for various filter combinations (e.g., $u - r$, $q - r$, $r - z$ etc) since they all track different ejecta coolants.

3. Discussion

With photometry, we can reduce the complexity of a nebular spectrum to just a few quantities (here mostly g, *^r*, and *ⁱ*). Secondary lines that are often used to constrain clumping or the temperature of the various emitting regions are no longer available (e.g., [Jerkstrand et al.](#page-4-17) [2015\)](#page-4-17). However, we hope in the future to construct our radiative transfer models from realistic 3D explosion models that would provide a physical measure of clumping, turbulence, and mixing, rather than craft one specific model for each observed SN. Another issue is line overlap, as can occur for [O I] $\lambda\lambda$ 6300, 6364 and [N II] $\lambda\lambda$ 6548, 6583 (or even possibly H α), and for [Ca II] $\lambda \lambda$ 7291, 7323 and [Ni II] λ 7378 in the 7300 Å emission feature. No information about this aspect will be available from the photometry. However, even with the spectra, we cannot evaluate the individual contributions from com-

Fig. 4. LSST $r - i$ color evolution for the Type Ibc simulations of [D21](#page-4-12) and Dessart et al. (in prep.) together with the counterpart for Type Ib SN 2004ao, and Type Ic SNe 2004gk and 2013ge [\(Modjaz et al.](#page-4-21) [2014;](#page-4-21) [Shivvers et al.](#page-4-22) [2019;](#page-4-22) [Drout et al.](#page-4-23) [2016\)](#page-4-23). The photometry is inferred from the spectra, by convolution with the LSST filter transmission curves, uncorrected for reddening or redshift – both are small. The data were retrieved from WISEREP [\(Yaron & Gal-Yam](#page-4-24) [2012\)](#page-4-24).

plicated blends, so the photometry will be no more ambiguous in that respect than the spectra. In contrast, photometry allows observations for a huge number of transients until late times with regular cadence and with better background subtraction than spectroscopy can provide. In that regard, photometry is better than spectroscopy.

As in spectroscopy, reddening will bring uncertainties. However, we may constrain the reddening from an inspection of the photometry and colors at early times, for example, around maximum light in SNe Ibc [\(Drout et al.](#page-4-25) [2011;](#page-4-25) [Dessart et al.](#page-4-26) [2016;](#page-4-26) [Woosley et al.](#page-4-27) [2021\)](#page-4-27). We show the color shift caused by a visual extinction of 1 mag, using the Cardelli law [\(Cardelli et al.](#page-4-28) [1989\)](#page-4-28) in Fig. [3.](#page-2-3) While reddening shifts the models up and to the right, the distinct trajectories are retained – it does not turn, for example, model he5p0 into model he8p0.

The observed photometric properties of a SN will be affected by its redshift. This redshift may be constrained in various ways: using existing spectroscopic redshifts of the host galaxies in the NASA/IPAC Extragalactic Database (NED) or from new host spectra; from photometric redshifts of the host galaxies (e.g., [Newman & Gruen](#page-4-29) [2022\)](#page-4-29); or from spectroscopic observations of the SN itself (e.g., [Blondin & Tonry](#page-4-30) [2007\)](#page-4-30). For redshift values below 0.1, most lines remain in the same filter as for zero redshift. At a redshift of 0.1, the strong lines lie between filters, in particular, for [O I] $\lambda\lambda$ 6300, 6364 and [Ca II] $\lambda\lambda$ 7291, 7323, so the method would not work in that case. However, for higher redshifts around 0.2, the strong lines fall again within a filter, with [O I] $\lambda\lambda$ 6300, 6364 now in *i* and [Ca II] $\lambda\lambda$ 7291, 7323 in *z*. Figure [A.3](#page-6-0) illustrates how the color–color magnitude diagram shown in Fig. [3](#page-2-3) is modified after redshift increments of 0.02.

At nebular times, the photometric evolution will also help in identifying some events or phenomena. Interaction with H-rich CSM will lead to a strong $H\alpha$ emission that will dominate the SN radiation, which will fall primarily in the *r* band (for zero redshift). A fast-evolving light curve with a persistent and dominant brightness in *^u* and g would be indicative of a Type Ibn [\(Pastorello et al.](#page-4-31) [2008;](#page-4-31) [Hosseinzadeh et al.](#page-4-32) [2017\)](#page-4-32).

Photometric analyses, along with their associated statistical analyses, will play an important role in analyzing and interpreting LSST SN data. However, it will still be important to obtain spectra for selected objects. For example, multi-epoch spectra could contribute a great deal to improving photometric modeling and interpretation, and in removing biases in photometric analyses. Further, modeling of SN spectra is still under development,

³ An offset between models and observations does not imply that the method is invalid but, instead, that the models are in tension with observations. The present models arise from a limited grid of theoretical models without any tuning. The numerous potential deficiencies of the models are discussed in [D21,](#page-4-12) and include the adoption of He-star models initially, the assumption of spherical symmetry in both the explosion models and in the radiative transfer, the neglect of clumping and molecule formation, the large abundance of stable Nickel explosively produced etc. Figures 23–27 in [D21](#page-4-12) show that these He-star explosion models (and their variants at higher/lower explosion energies – see [D21](#page-4-12) for details) reproduce satisfactorily the representative spectra of SNe IIb, Ib, and Ic so they evidently also reproduce the corresponding photometry.

and thus high quality spectra (over a large passband) throughout a SN evolution, combined with high quality photometric data, will be needed to test the radiative-transfer models.

Setting a focus on the color evolution would take a more global look at the evolution and properties of SN Ibc ejecta, as opposed to a line-by-line analysis with spectra. This a different, and in many respects, a complementary approach to spectroscopy, with numerous merits and strengths nonetheless. The LSST will soon be in operation and we ought to extract the information encoded in that rich photometric data.

4. Conclusion

We present the nebular-phase radiative properties of a wide range of He-star explosions that cover both standard Type Ibc SNe and faint, currently unknown, Type Ib SNe that arise from the lowest mass He stars undergoing core collapse [\(Woosley](#page-4-15) [2019;](#page-4-15) [D21\)](#page-4-12). To complement previous studies that focus almost exclusively on spectral properties [\(Jerkstrand et al.](#page-4-17) [2015;](#page-4-17) [D21;](#page-4-12) Dessart et al., in prep.), we have set our focus on their photometric properties. This is motivated by the growing number of transients that have primarily photometric data, with little or no spectroscopic information. With this in mind, we framed our discussion on the LSST and its *^u*g*riz* filters to assess how photometry can help us constrain the progenitors and ejecta of Type Ibc SNe.

The most significant plot in this work is the $r - i$ versus $q - r$ color–color magnitude diagram for the simulations of [D21](#page-4-12) and Dessart et al. (in prep.; Fig. [3\)](#page-2-3). This figure shows how each family of He-star explosions from [D21](#page-4-12) occupies a different parameter space, and how each follows a distinct trajectory over time. For redshifts below about 0.07, the filters g, *^r*, and *ⁱ* cover the spectral regions where the primary coolants of the various shells emit. The He-rich material, which cools through Fe II emission below 5500 Å, is captured by the q band. The O-rich material increasingly cools through [O I] $\lambda\lambda$ 6300, 6364 during the first one to two years after explosion and that emission is covered by the *r* band. Finally, radiation from the Fe-rich and Si-rich material comes out primarily in $\left[$ Ca II $\right]$ λ λ 7291, 7323, which falls within the *i* band. Different proportions of these various shell masses lead to a distinct color evolution. What is lost with the lack of spectra is also compensated for by the more extensive monitoring at all epochs with the LSST. The *^u*g*rizy* filter set is also much more extended in wavelength than most SN spectra, which are typically truncated in the blue and often in the red.

The photometric approach will also allow SNe to be studied until much later times, an endeavor that has been possible only with the most nearby events such as the Type IIb SN 1993J. Furthermore, it will be possible to capture the onset of an interaction with CSM, as evidenced through a sudden reduction of *u*−*r* color [\(Dessart & Hillier](#page-4-33) [2022\)](#page-4-33).

Obviously, degeneracies that affect SN Ibc spectra will also affect their photometry. Recently, [Fang et al.](#page-4-34) [\(2022\)](#page-4-34) and [Prentice et al.](#page-4-35) [\(2022\)](#page-4-35) presented an analysis of nebular-phase spectra of SNe Ibc and revealed the absence of a clear correlation between the flux ratio of [O I] $\lambda\lambda$ 6300, 6364 and [Ca II] $\lambda \lambda$ 7291, 7323 in their Type Ibc SN sample, which conflicts with the common expectation that Type Ib and Type Ic SN progenitors have different (increasing) O content. Obviously, a photometric analysis would similarly reveal a lack of correlation in $r - i$ for this sample. Physically, there may be various reasons for this lack of correlation. First, while SNe Ic may arise from higher mass progenitors on the main sequence than SNe Ib, the effect of wind mass loss might lead to a relatively narrow range of preSN masses [\(D21\)](#page-4-12). Second, the sample of observed SNe Ibc seems to lack low-mass He-rich ejecta with very weak [O I] $\lambda\lambda$ 6300, 6364 (corresponding to our models he2p6–he4p0), while higher mass ejecta with several solar masses of O are unfavored by the initial mass function and may, thus, be more scarce. What may then drive the currently observed diversity between and amongst SNe Ib and Ic is not, perhaps, a difference in composition, as generally assumed but, instead, the large-scale macroscopic mixing of ⁵⁶Ni and other elements such as He and O [\(Dessart et al.](#page-4-36) [2012\)](#page-4-36). Further work is needed to address this issue in stripped-envelope SNe. Crucially, LSST photometry, along with color–color diagrams formed from that photometry, will provide strong statistical constraints on SN properties and the progenitors that give rise to these SNe, with the potential to address this issue directly.

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Appendix A: Additional figures

Figure [A.1](#page-5-0) illustrates the close correspondence between the ratio of the combined [O I] $\lambda\lambda$ 6300, 6364 and [N II] $\lambda\lambda$ 6548, 6583 fluxes with that of [Ca II] $\lambda \lambda$ 7291, 7323 and the color $r - i$ shown in Fig. [2.](#page-2-1) If we were to omit the lower mass He-star explosion models, the color $r - i$ would reflect the ratio of the [O I] $\lambda\lambda$ 6300, 6364 and the [Ca II] $\lambda\lambda$ 7291, 7323 line fluxes, with a slight offset due to the neglect of the overlapping iron and nickel emission [\(D21;](#page-4-12) Fig. [A.2\)](#page-5-1).

Figure [A.2](#page-5-1) shows the spectral evolution for the low-mass model he2p6 and the high-mass model he8p0 from 100 to about 450 d after explosion. A detailed description of the spectral properties is given in D21 and in Dessart et al. (in prep.).

Figure [A.3](#page-6-0) shows how the model trajectories in the color– color magnitude diagram of Fig. [3](#page-2-3) are modified after successive redshift increments of 0.02. For redshifts below about 0.06, the strongest spectral lines remain within the same LSST filter as for a redshift of zero. Increasing the redshift to 0.1 leads to significant changes because the strong emission lines in *r* and *i* approach and cross the edge of these filters. Nonetheless, the respective models are still distinguishable.

Fig. A.1. Evolution of the ratio of the combined [O I] $\lambda\lambda$ 6300, 6364 and [N II] $\lambda\lambda$ 6548, 6583 fluxes with that of [Ca II] $\lambda\lambda$ 7291, 7323 for models he2p6, he4p0, he5p0, he6p0, he8p0, and he12p0. These curves are analogous to the $r - i$ color curves shown in Figs. [2](#page-2-1) and [4.](#page-3-1)

Fig. A.2. Evolution of the optical spectrum of model he2p6 (left) and he8p0 (right) from 100 to about 450 d. Overplotted is the contribution from bound-bound transitions associated with various ions. The spectrum that includes all Fe I, Fe II, and Fe III bound-bound transitions is labeled by the key "Iron".

Fig. A[.3](#page-2-3). Same as Fig.3 but for redshift increments of 0.02 from 0 at top left to 0.1 (bottom right).